

Numerical Modelling of the Damage Potential of Indoor Climate Variations to a Historic Wooden Cabinet

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Where innovation starts

#### Introduction

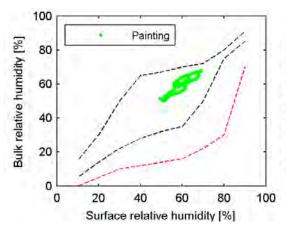
#### **Museum objects**

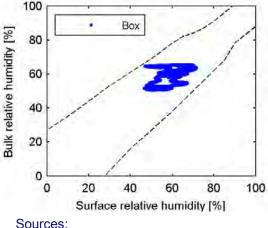
Risks of biological, chemical and mechanical degradation due to wrong indoor climate conditions

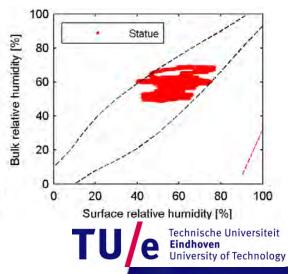


#### Prediction of mechanical stress related to climate variations

- Analysis of hygroscopic and mechanical behaviour of objects
- Definition of tolerable fluctuations of relative humidity







Panel painting: Mecklenburg et al. (1998) Lacquer Box: Bratasz et al. (2009) Wooden Statue: Kozlowski (2007)

Graphical representation: Martens (2011)

# Case study

#### **Van Mekeren Cabinet**

- Situated in Grand Salon, Amerongen Castle, The Netherlands
- Created by Jan van Mekeren around 1690-1710









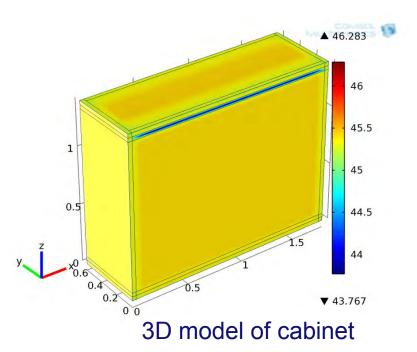
### **Objectives**

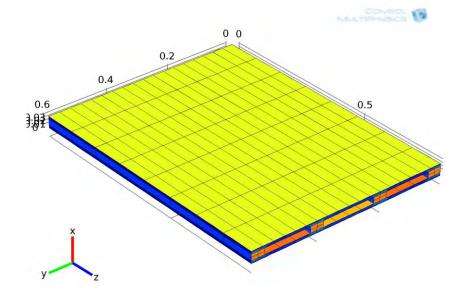
- To analyse the response time of a door panel to a sudden relative humidity increase
- To analyse the microclimate conditions around the cabinet as a results of the indoor climate conditions in the Grand Salon
- To predict deformation of a door panel due to climate variations
- → Validation with on-site measurements



# **COMSOL** modelling

- Heat transfer in solids and fluids module
- Structural mechanics module





3D model of door panel



# **COMSOL** modelling

Heat and moisture transport

$$\rho c_p \frac{\partial T}{\partial t} = \nabla (k \nabla T)$$

$$\frac{\partial Pv}{\partial t} = \nabla (D(Pv)\nabla Pv)$$

```
ho = density [kg/m³]

c_p = specific heat capacity [J/kgK]

T = temperature [°C]

K = thermal conductivity [W/mK]

Pv = vapour pressure [Pa]

D(P) = moisture diffusion coefficient [m²/s]
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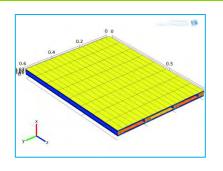
### **COMSOL** modelling

#### Stress and strain

$$\begin{pmatrix} \varepsilon_{x} \\ \varepsilon_{y} \\ \gamma_{xy} \end{pmatrix} = \begin{pmatrix} \frac{1}{E_{x}} & -\frac{v_{xy}}{E_{Y}} & 0 \\ -\frac{v_{yx}}{E_{x}} & \frac{1}{E_{y}} & 0 \\ 0 & 0 & \frac{1}{G_{xy}} \end{pmatrix} \begin{pmatrix} \sigma_{x} \\ \sigma_{y} \\ \tau_{xy} \end{pmatrix} + \begin{pmatrix} \alpha_{x} \\ \alpha_{y} \\ 0 \end{pmatrix} \Delta\theta + \begin{pmatrix} \kappa_{x} \\ \kappa_{y} \\ 0 \end{pmatrix} \Delta w$$

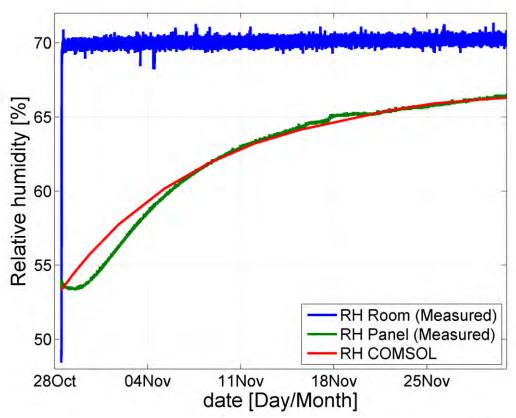
```
\begin{array}{lll} \epsilon_x \epsilon_y & = & \text{normal strain components [-]} \\ \gamma_{xy} & = & \text{shear strain component associated with two axis [-]} \\ v_{xy}, v_{yx} & = & \text{Poisson's ratio [-]} \\ E_x, E_y & = & \text{Young's moduli [N/m²]} \\ G_{xy} & = & \text{shear modulus [N/m²]} \\ \alpha_x, \alpha_y & = & \text{linear thermal expansivity [m/mK]} \\ \theta & = & \text{temperature [°C]} \\ \kappa_x, \kappa_y & = & \text{linear deformation due to changes in moisture content [m/m(kg/m³)]} \\ w & = & \text{moisture content [kg/m³]} \end{array}
```

### Response time



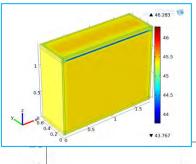
#### **Test chamber experiment**

- Sudden relative humidity increase from 50% to 70%
- Temperature is maintained constant at 20°C



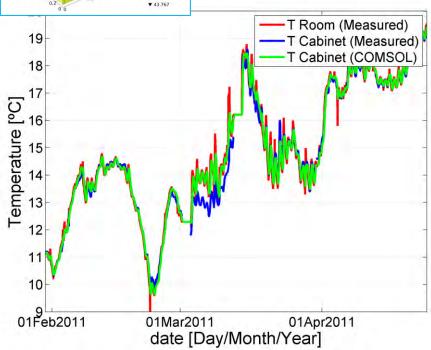
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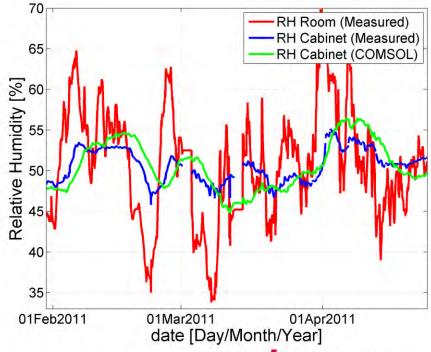
#### **Microclimate conditions**



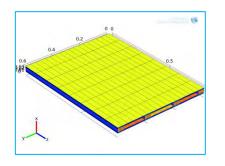
# On-site measurements of temperature and relative humidity in Grand Salon and inside cabinet

 Comparison between measured and simulated microclimate conditions in COMSOL

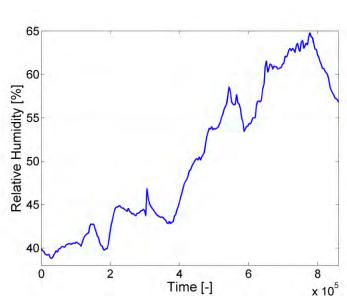




### Deformation

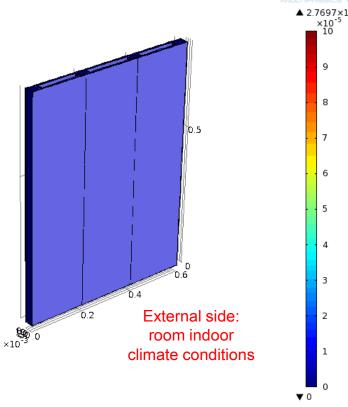


#### **Predicted displacement during 10 days**

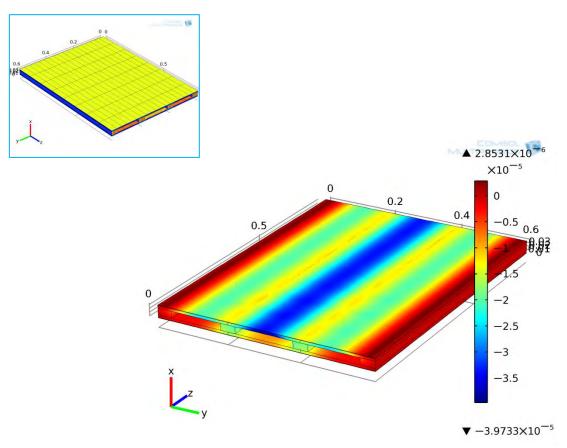


Internal side: microclimate conditions cabinet

Time=0 Surface: Total displacement Total displacement (m)



### **Deformation**

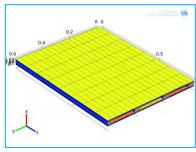


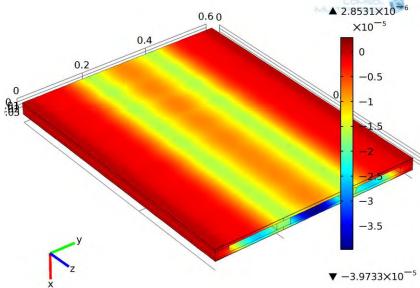
Predicted deformation at external side t =1000





# **Deformation**





Predicted deformation at internal side t=1000



#### Conclusions

- Response time of door panel is adequately predicted
- Modelling of microclimate conditions requires improvement
- Agreement is found between predicted deformation and visible damage
- More detailled measurements of hygroscopic and mechanical properties of the various wood types in the cabinet are necessary to calculate stress and strain in the cabinet as a result of climate variations



Thank you for your attention



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