

Complex k-bands of plasmonic crystal slabs

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Introduction: We present a Finite Element Method (FEM) to calculate the complex valued $\mathbf{k}(\omega)$ dispersion curves of a *plasmonic crystal slab* in presence of both dispersive and lossy materials. The method can be exploited to study plasmonic crystal slabs.

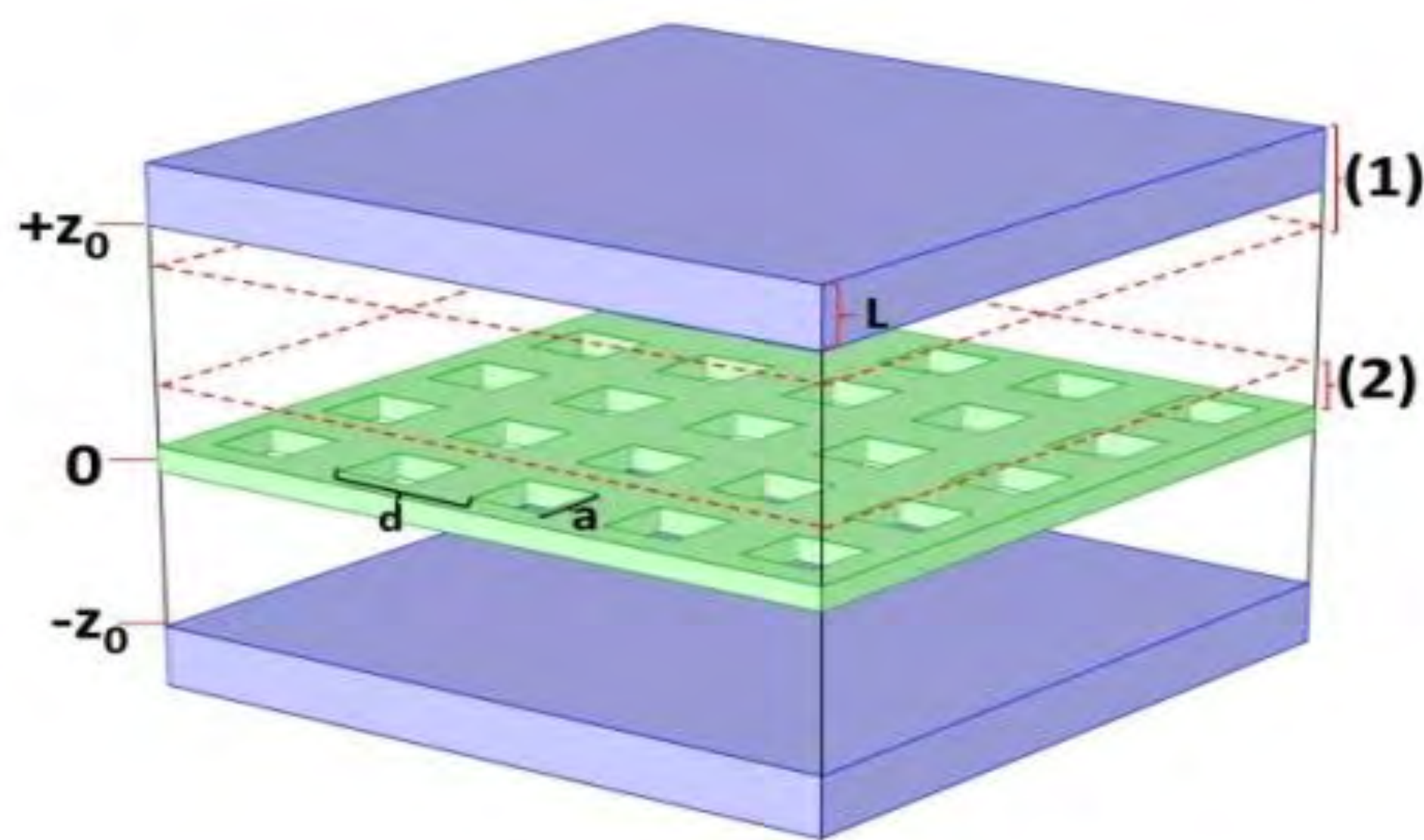


Figure 1. Unite cell

Computational Methods: The method relies on the *weak formulation* of the Helmholtz's eigenvalue equation [1,2,3]. :

$$\begin{cases} \nabla \times (\hat{p} \nabla \times \mathbf{H}) - \omega^2 \hat{q} \mathbf{H} = 0 & \hat{p} = 1/\hat{\mu}(\mathbf{r}, \omega), \quad \hat{q} = \hat{\epsilon}(\mathbf{r}, \omega) \\ \mathbf{H} = e^{-i\mathbf{k} \cdot \mathbf{r}} \mathbf{u}(\mathbf{r}) & \mathbf{u}(\mathbf{r}) \text{ Bloch function, } \mathbf{k} \text{ eigenvalue} \end{cases}$$

$$\int_{\Omega} d^3\mathbf{r} \left(\hat{p} \left[k^2 (\mathbf{v} \cdot \mathbf{u}) - (\mathbf{k} \cdot \mathbf{v})(\mathbf{k} \cdot \mathbf{u}) \right] - i\hat{p}\mathbf{v} \cdot [\mathbf{k} \times (\nabla \times \mathbf{u})] - i(\nabla \times \mathbf{v}) \cdot \hat{p}(\mathbf{k} \times \mathbf{u}) \right) + \int_{\Omega} d^3\mathbf{r} \left((\nabla \times \mathbf{v}) \cdot \hat{p}(\nabla \times \mathbf{u}) - \hat{q} \frac{\omega^2}{c^2} \mathbf{v} \cdot \mathbf{u} \right) + \int_{\partial\Omega} dA \mathbf{v} \cdot [\hat{\mathbf{n}} \times \hat{p}(-i\mathbf{k} \times \mathbf{u} + \nabla \times \mathbf{u})] = 0,$$

In order to deal with leaky modes and to simulate Perfect Matched Layers (PML) an anisotropic tensor is required in the form of:

$$\hat{\epsilon} = \epsilon \hat{\Lambda}, \quad \hat{\mu} = \mu \hat{\Lambda}, \quad \hat{\Lambda} = \begin{pmatrix} c & 0 & 0 \\ 0 & c & 0 \\ 0 & 0 & c^{-1} \end{pmatrix},$$

$$\begin{cases} c = \alpha - i\beta \\ \beta = \bar{\sigma} \frac{|(z \mp |z_0|)|^n}{L^n} \end{cases} \cdot \kappa = \frac{\langle |\mathbf{H}|^2 \rangle_{(1)}}{\langle |\mathbf{H}|^2 \rangle_{(2)}}$$

Results: The figures below show the retrieved results: the TE and TM modes compared with Transmittance maps (Fig. 2 ,3 respectively), the H_y and $|\mathbf{E}|$ fields profiles (Fig.4) and the imaginary part of modes eigenvalues (Fig.5)

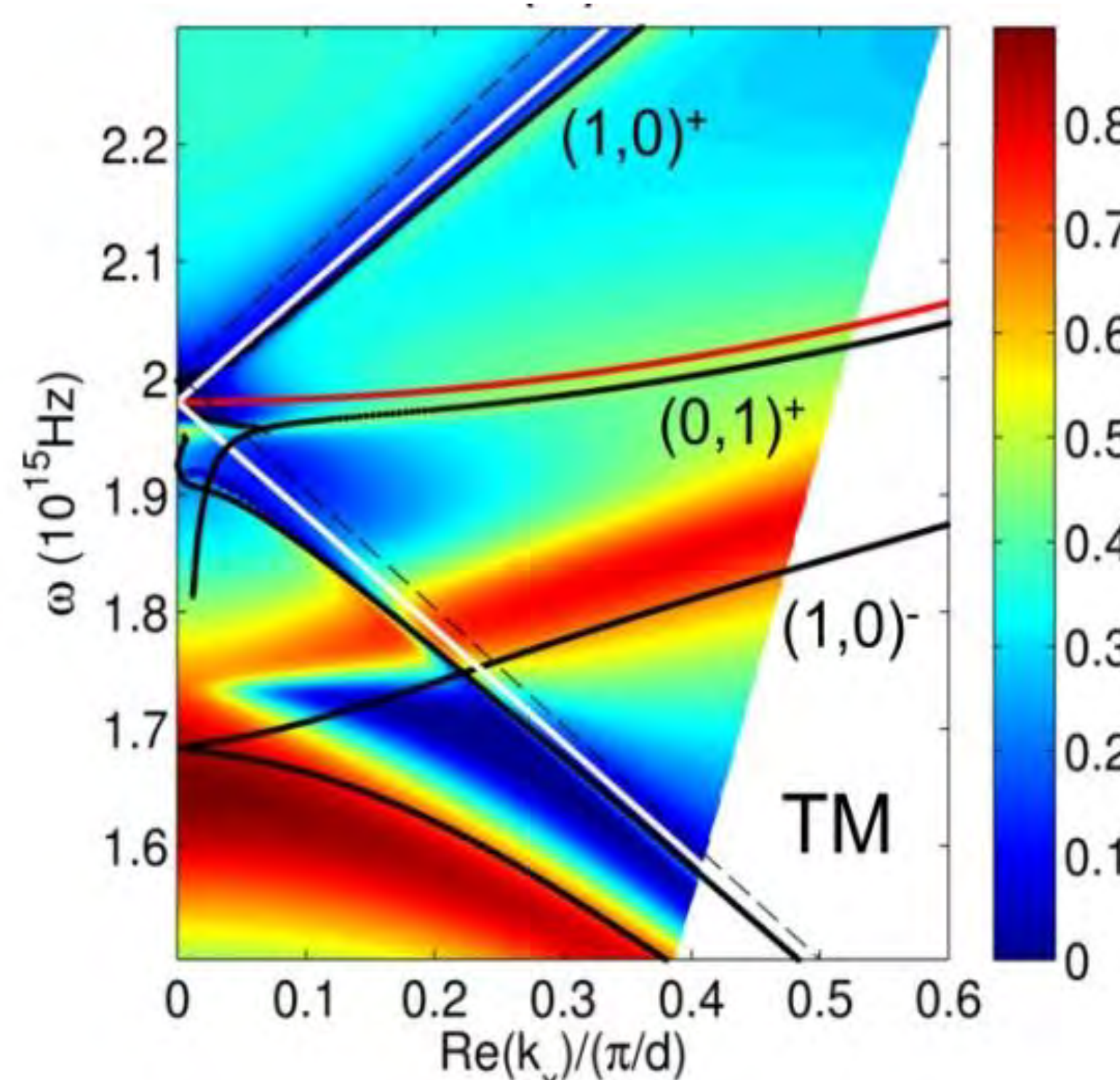


Figure 2. TM modes

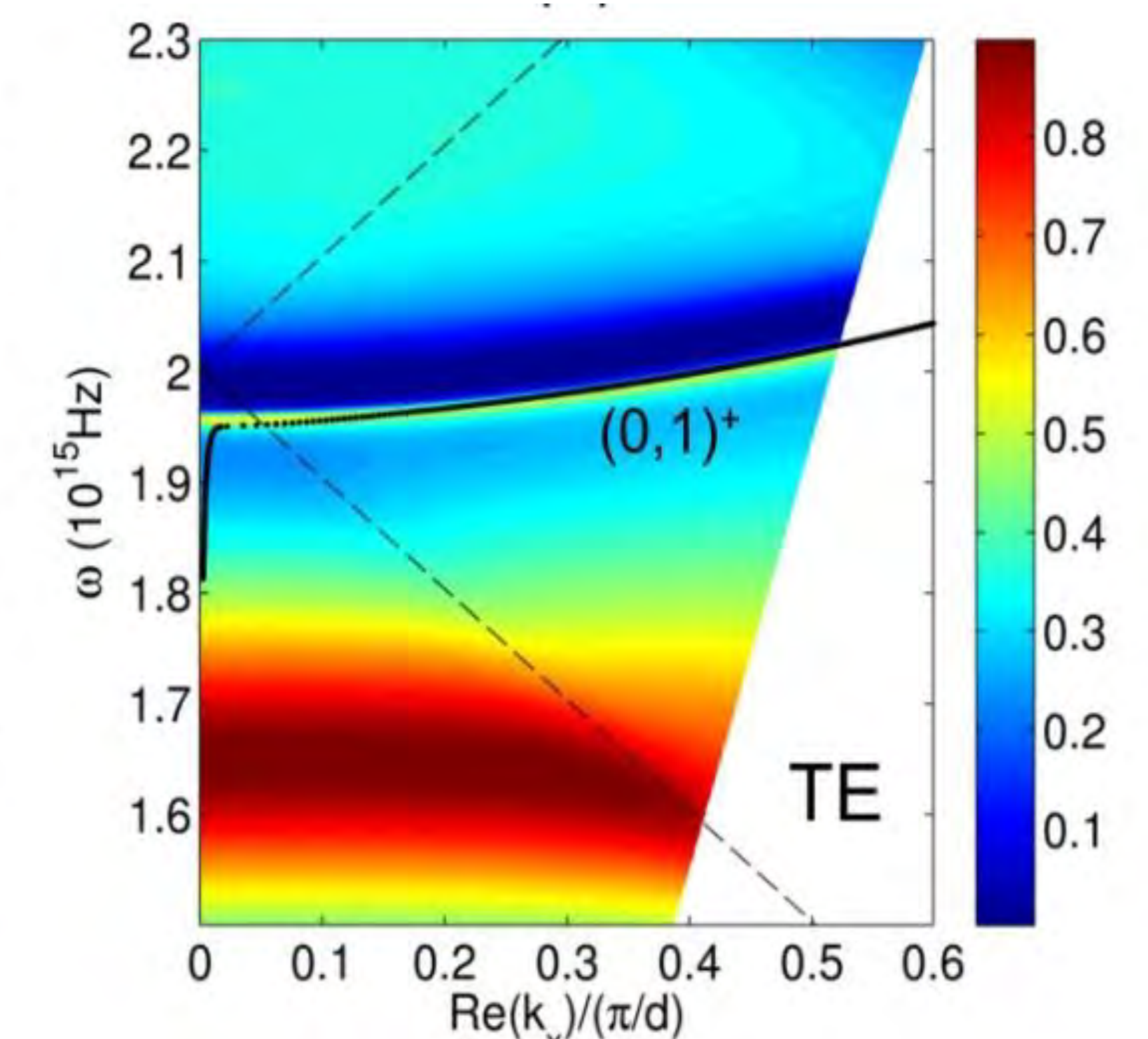


Figure 3. TE modes

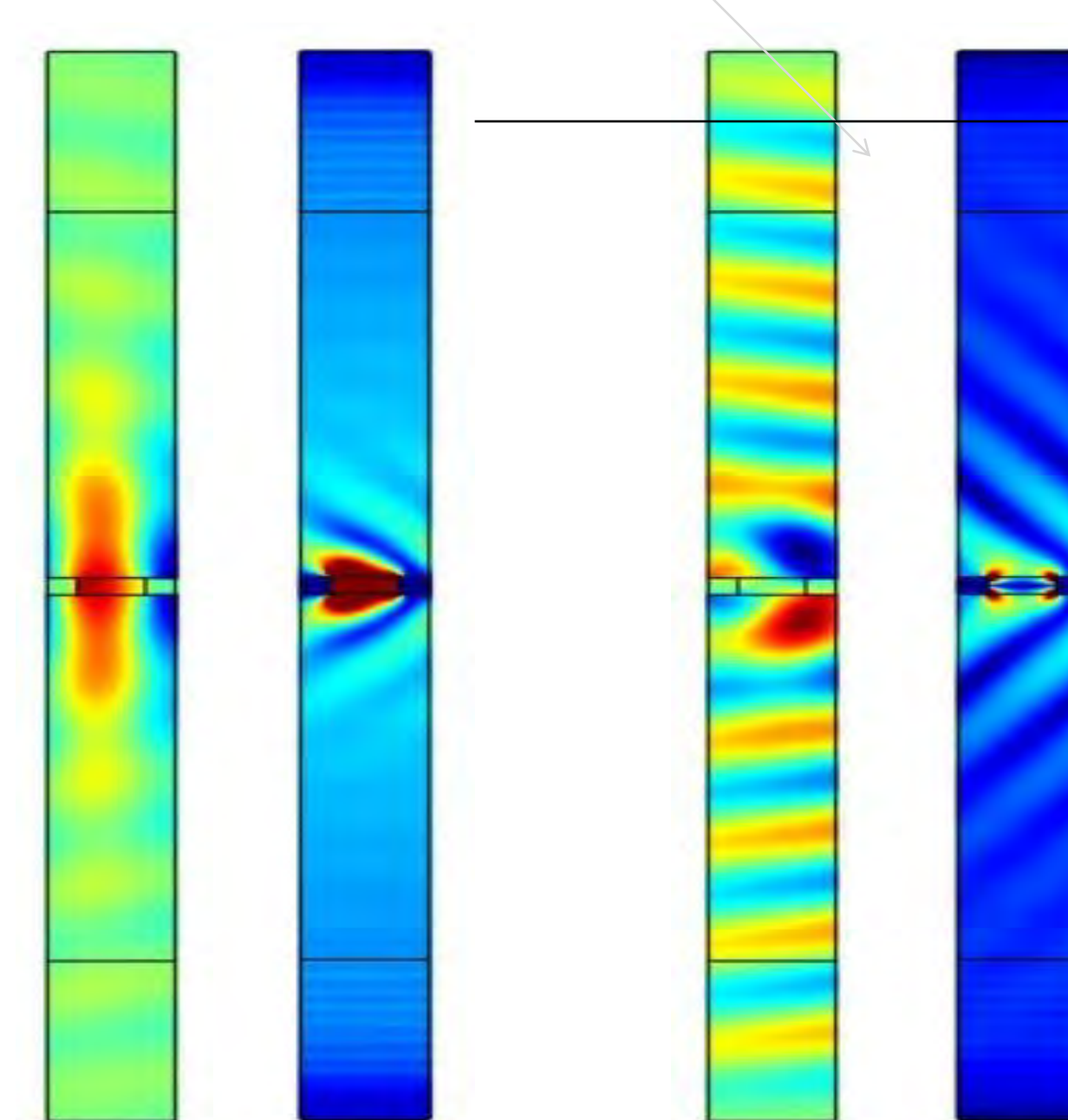


Figure 4. H_y and $|\mathbf{E}|$ fields

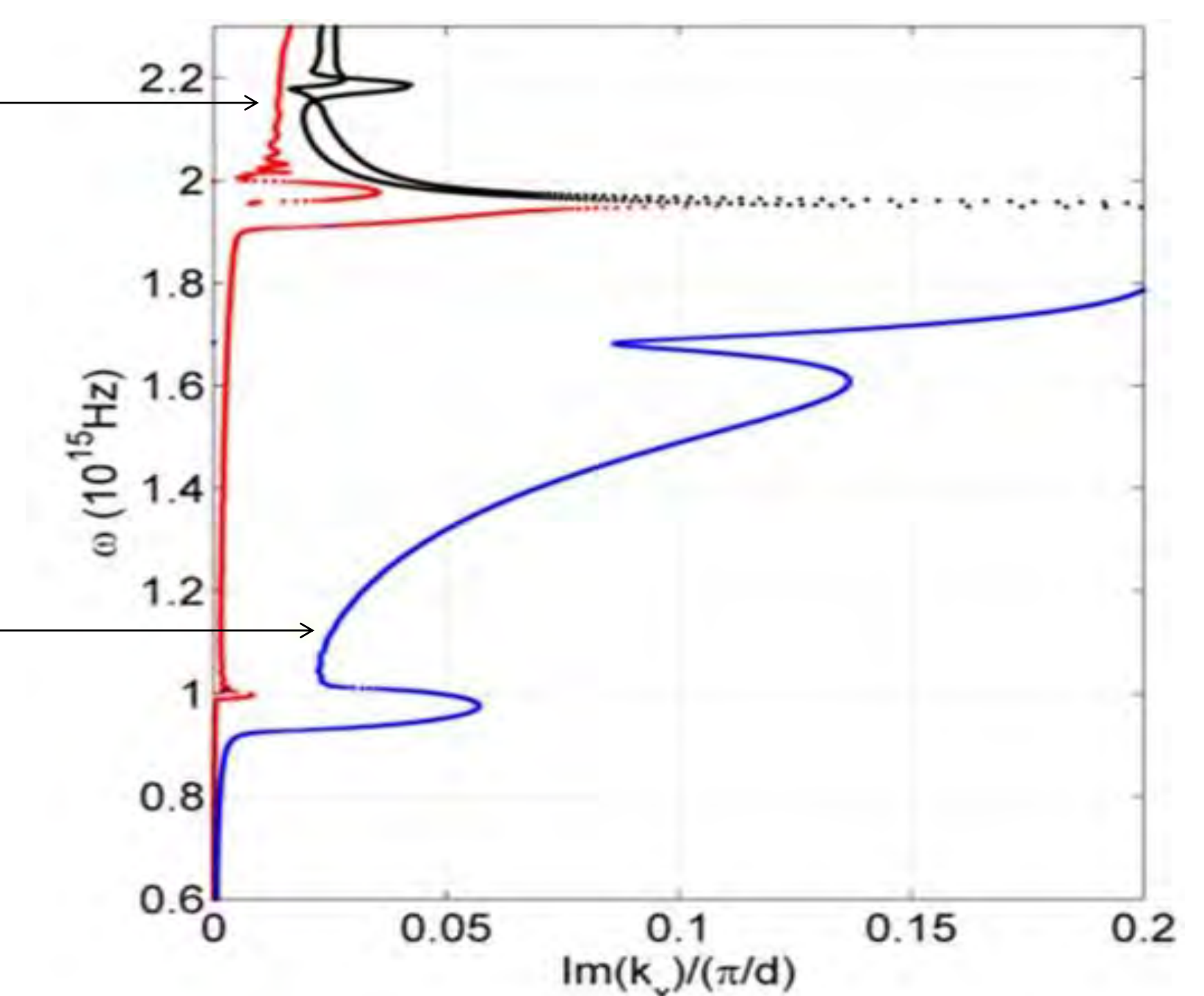


Figure 5. Imaginary k bands

Conclusions: Our results prove that PML implementation allows to effectively study leaky modes, characteristic features of photonic crystal slabs, thus enabling the reconstruction of the correct radiative eigenmode profile.

References:

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3. C. Fietz, "Complex k band diagrams of 3D metamaterials/photonic crystals," *Opt. Express*, **19**, 19027-19041 (2011).