



Gravitational Collapse of Rectangular Granular Piles

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Presentation Outline

- **Introduction, Motivation & Background**
- **Constitutive Relations**
- **Numerical Solution**
- **Material Properties & Investigated Geometries**
- **Results**
 - **Evolution of Slump Shapes**
 - **Comparison with Experimental Data**
- **Summary & Conclusions**



Introduction

- **Flow & collapse of granular materials:**
 - **Industry:**
 - **Agriculture**
 - **Pharmaceuticals**
 - **Petroleum & Mining**
 - **Geophysical processes:**
 - **Landslides**
 - **Avalanches**



Motivation & Background

- **Available Literature**
 - **Experimental**
 - **Geometries (2D Symmetric, 2D dam-break, Semi-Axisymmetric, Axisymmetric)**
 - **Materials (sand, glass beads, rice, sugar, ...)**
 - **Basal conditions (rough and/or smooth bottom)**
 - **Numerical**
 - **Usually depth-averaged equations, shallow-water approximation**
 - **Collapse of short-thick blocks; NOT tall-thin blocks**



Constitutive Relations & Governing Equations

- **Modified von Mises yield function**
- **Isotropic**
- **Associated flow rule**
- **Incompressible**
- **Plane strain**



- **Stress-strain rate relationship:**

$$\sigma_{ij} = \sigma_m \delta_{ij} - \left(\dot{\epsilon}_{ij} - \dot{\epsilon}_{kk} \delta_{ij} / 3 \right) \sigma_m \sin \phi / (I_2)^{0.5}$$

- **The granular material is a fluid with the dynamic shear viscosity of:**

$$\eta = p \sin \phi / \left(2(I_2)^{0.5} \right) \longrightarrow \eta = \alpha + p \sin \phi / \left(2(\beta + I_2)^{0.5} \right)$$

Numerical Stability



Numerical Solution

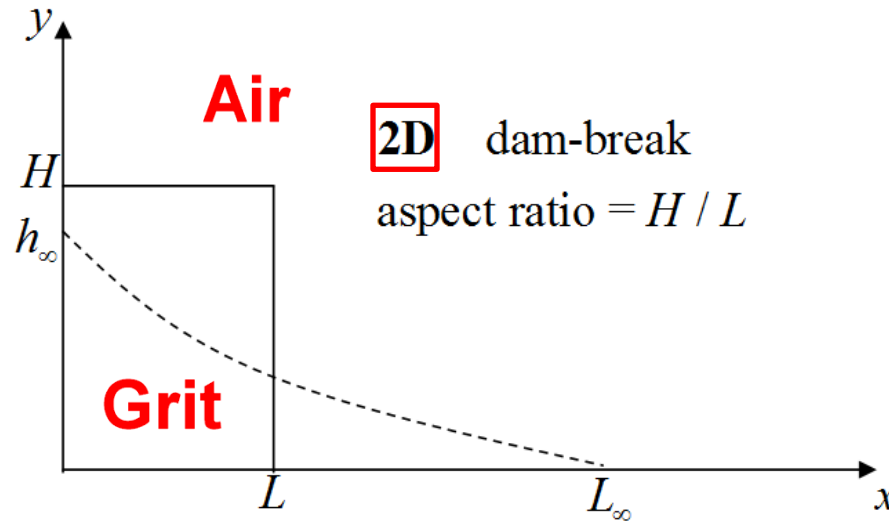
- **COMSOL FE tool (version 4.2a), CFD two-phase laminar flow module**
- **The Level-Set method was used to track the interface between the two phases**



Granular Material

- Grit, irregular grain shapes, mean size 1 mm.

| Grit | Surrounding Air |
|-------------------------------|-----------------------------------|
| $\phi_{grit} = 34^\circ$ | $\eta_{air} = 10^{-5} Pa \cdot s$ |
| $\rho_{grit} = 2600 kg / m^3$ | $\rho_{air} = 1 kg / m^3$ |

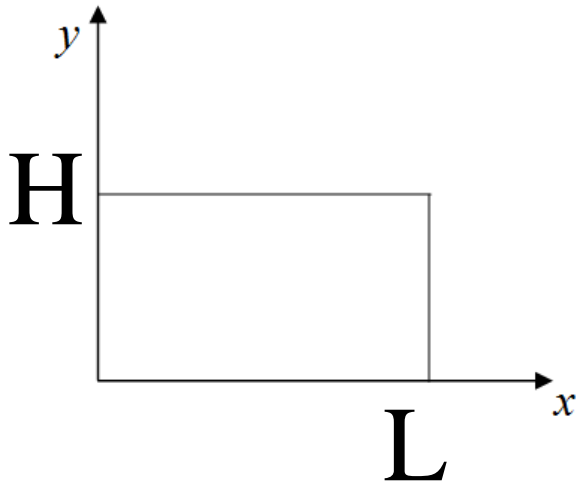


Geometries

Case I (*short – thick*)

$$H = 10 \text{ cm}$$

$$L = 20 \text{ cm}$$

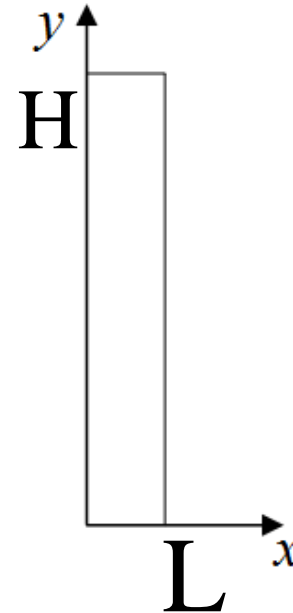


aspect ratio = 0.5

Case II (*tall – thin*)

$$H = 25 \text{ cm}$$

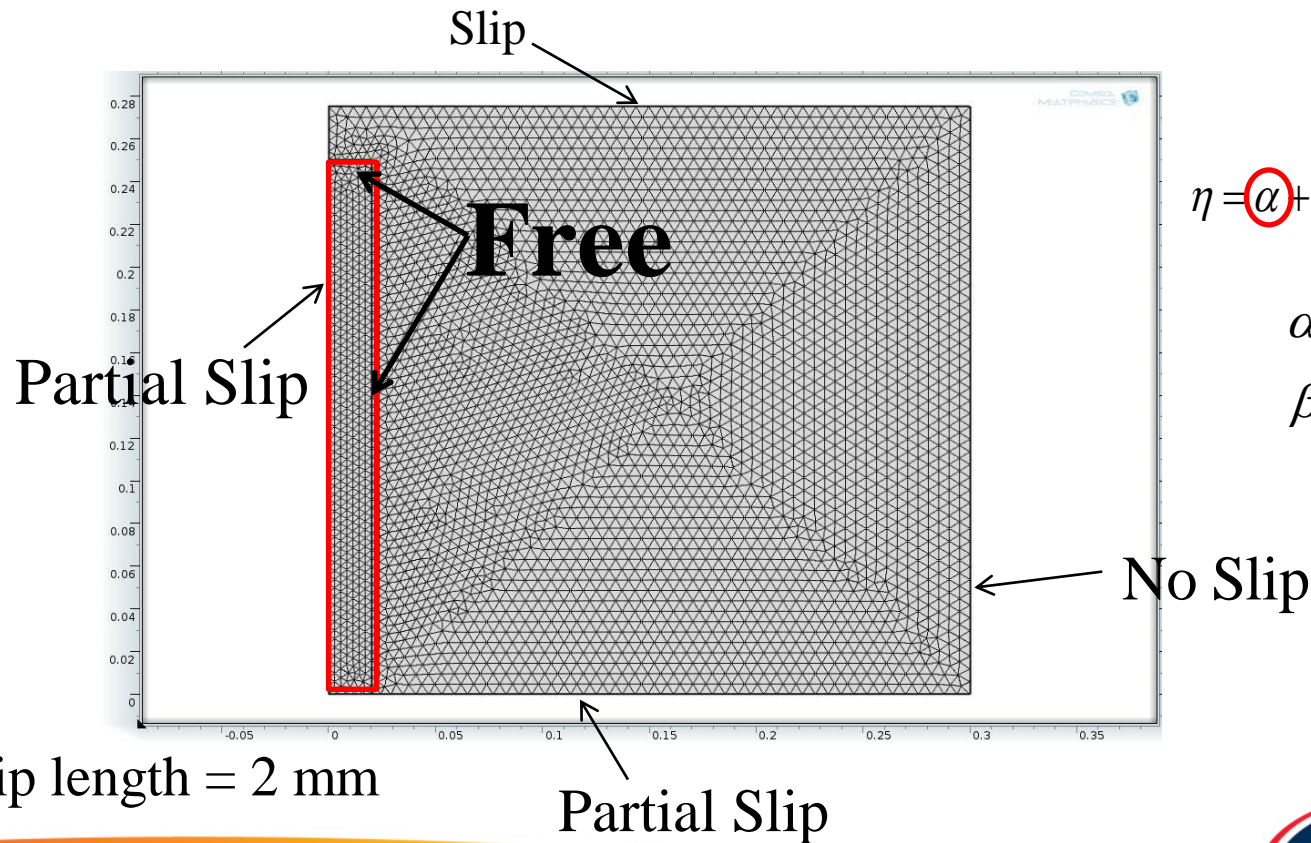
$$L = 2 \text{ cm}$$



aspect ratio = 12.5

Results

- Triangular mesh, element size is approximately 4 mm



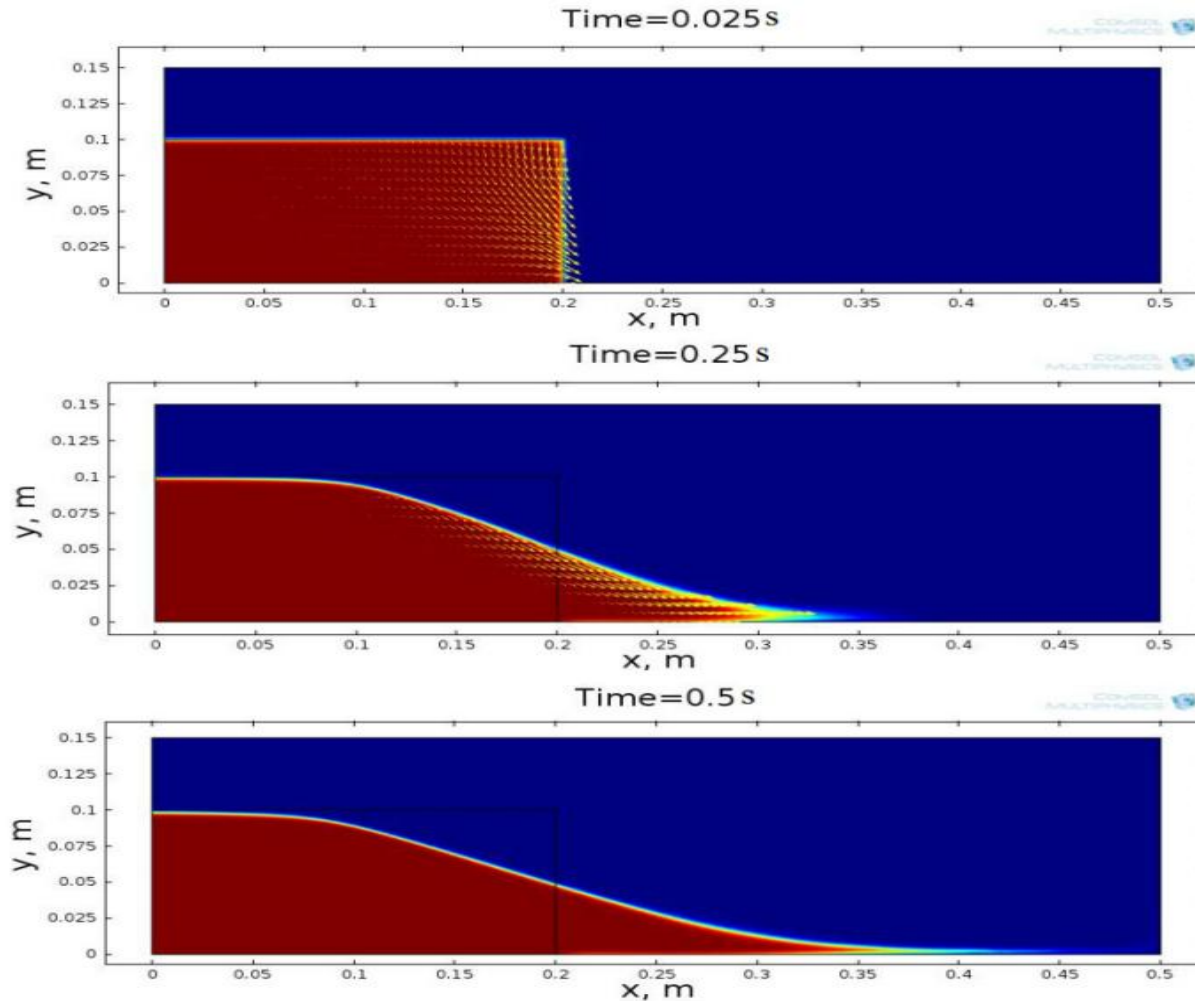
$$\eta = \alpha + p \sin \phi / (2(\beta + I_2)^{0.5})$$

$$\alpha = 1 \text{ Pa} \cdot \text{s}$$

$$\beta = 0.075 \text{ s}^{-2}$$

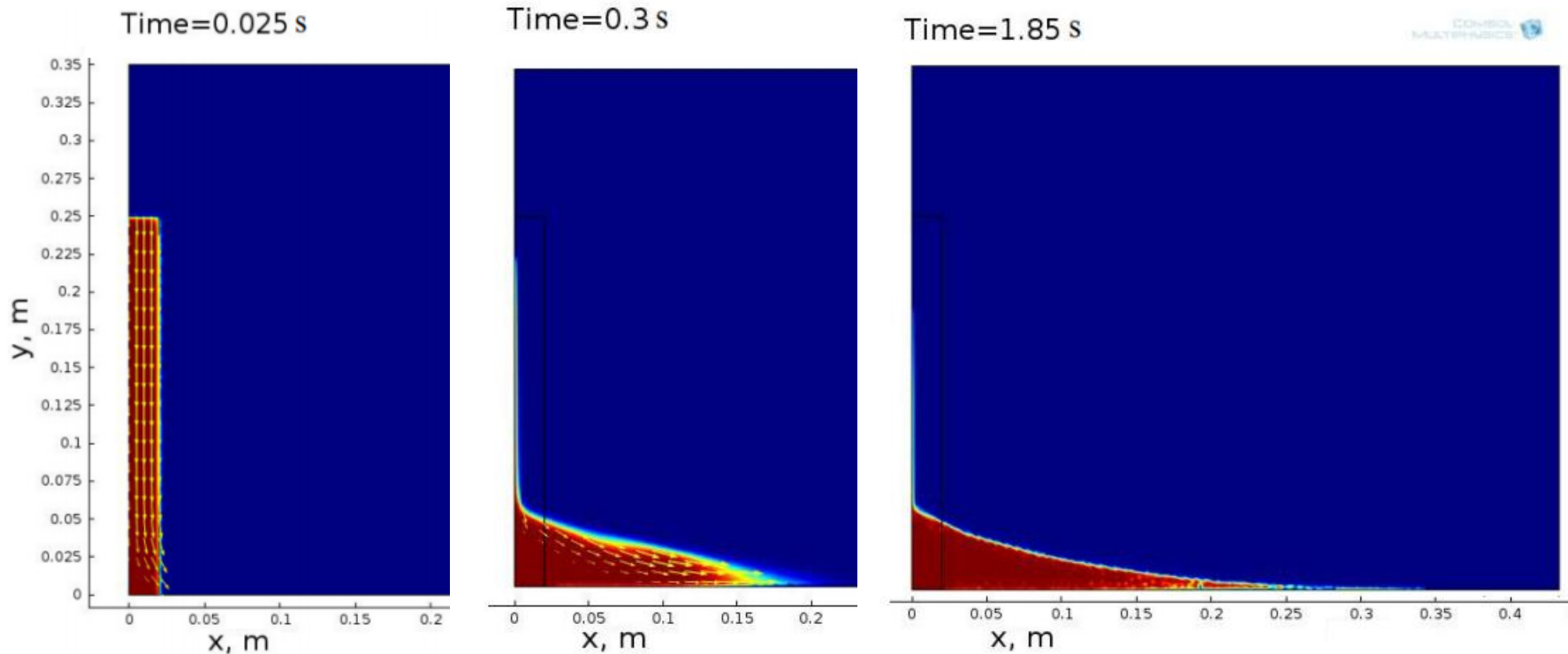
Evolution of Slump Shapes

- CASE I, Low Aspect Ratio Pile



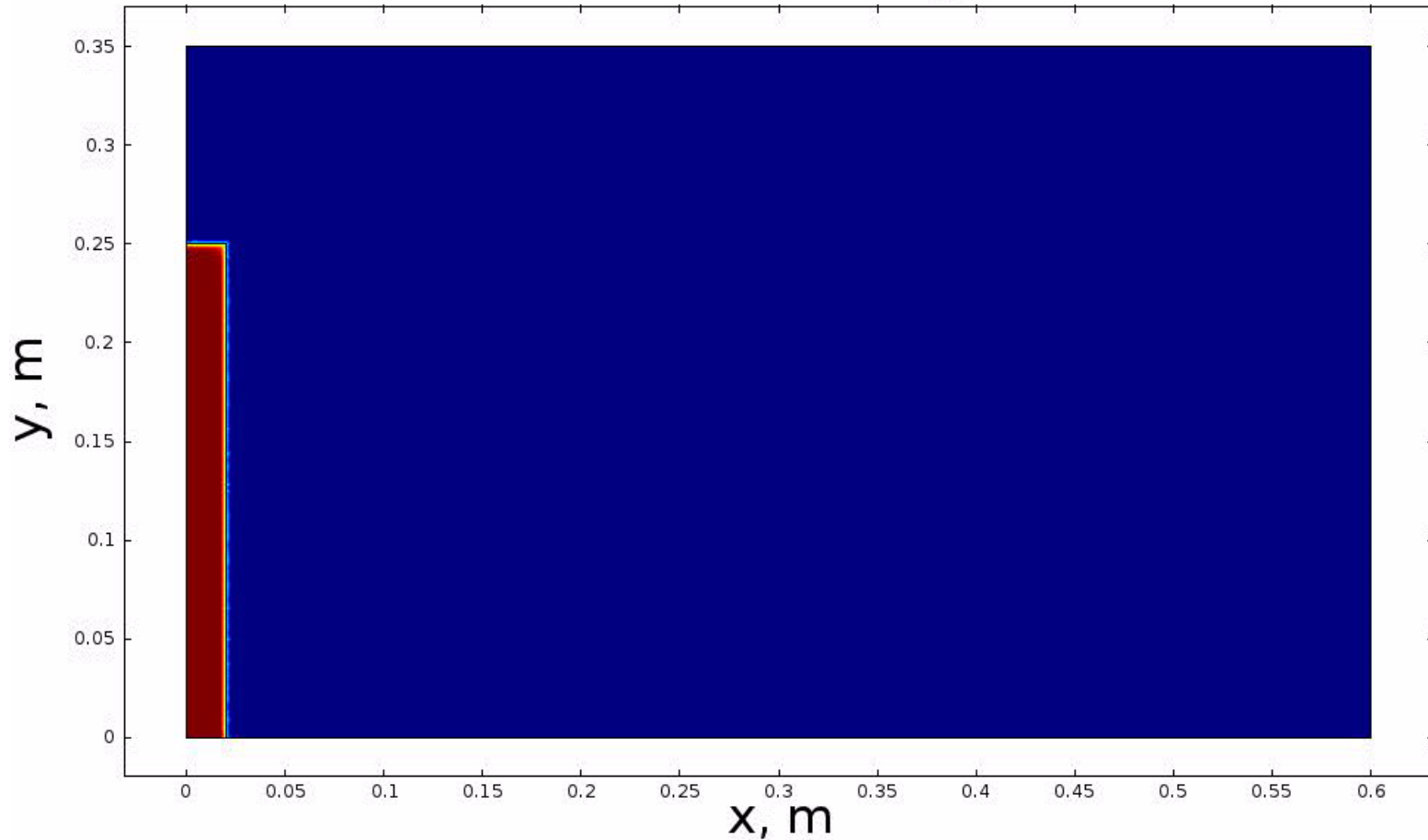
Evolution of Slump Shapes

- CASE II, High Aspect Ratio Pile



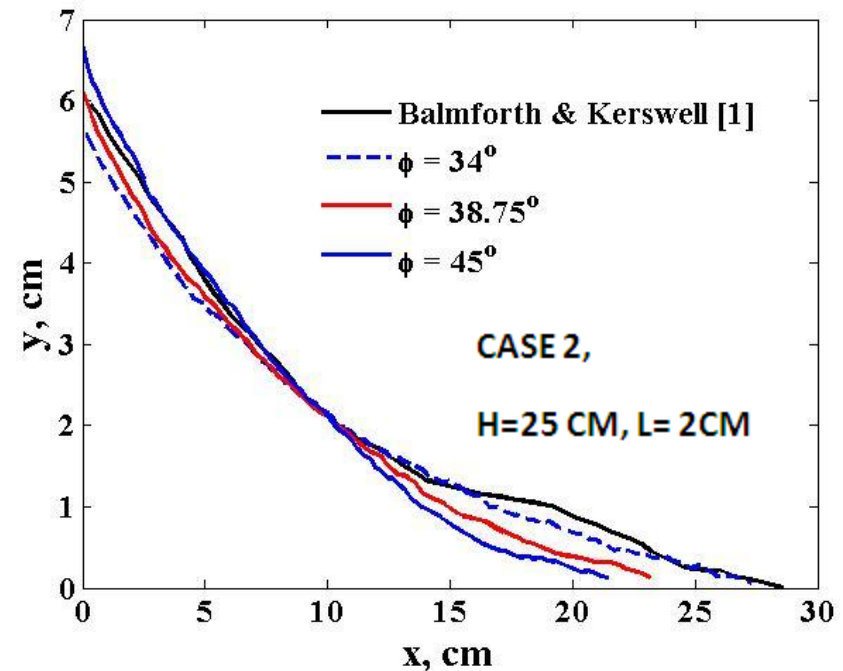
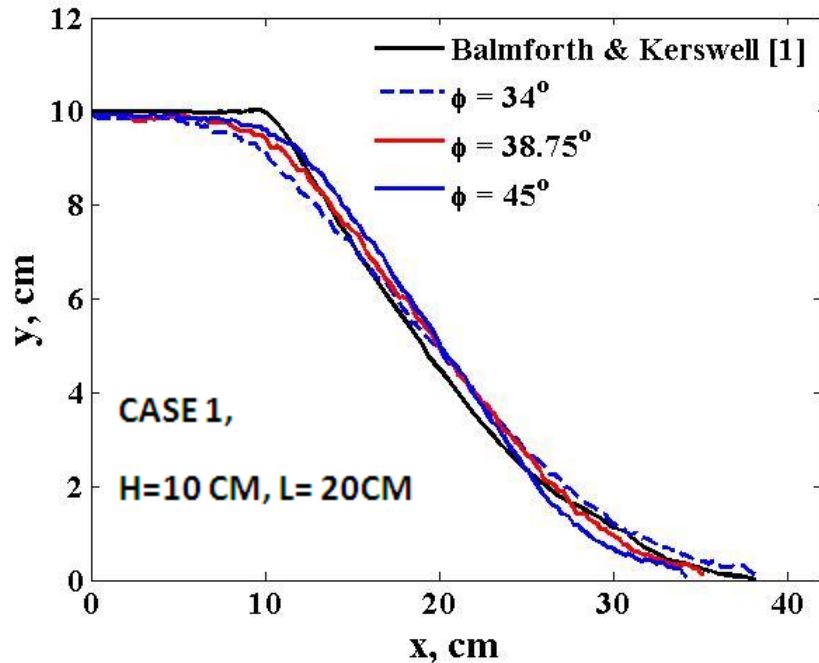
→
increasing time

Time=0 Volume fraction of grit



Comparison with Available Experiments

- Close prediction of the final runout, final height, and the final free surface profile
- An increase in the internal angle of friction reduces the runout



Final profiles

Summary & Conclusions

- **Mohr-Coulomb based constitutive relations**
- **Strain-rate and pressure dependent shear viscosity**
- **Two-phase flow problem**

- **Partial slip at boundaries in contact with the granular material**

- **Stable heaps are captured**
- **Final free-surface profiles agree with experiments**





Thank you!



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