

AMPHOS²¹
SCIENTIFIC AND STRATEGIC ENVIRONMENTAL CONSULTING

CO₂ Storage Trapping Mechanisms Quantification

COMSOL
CONFERENCE
ROTTERDAM2013

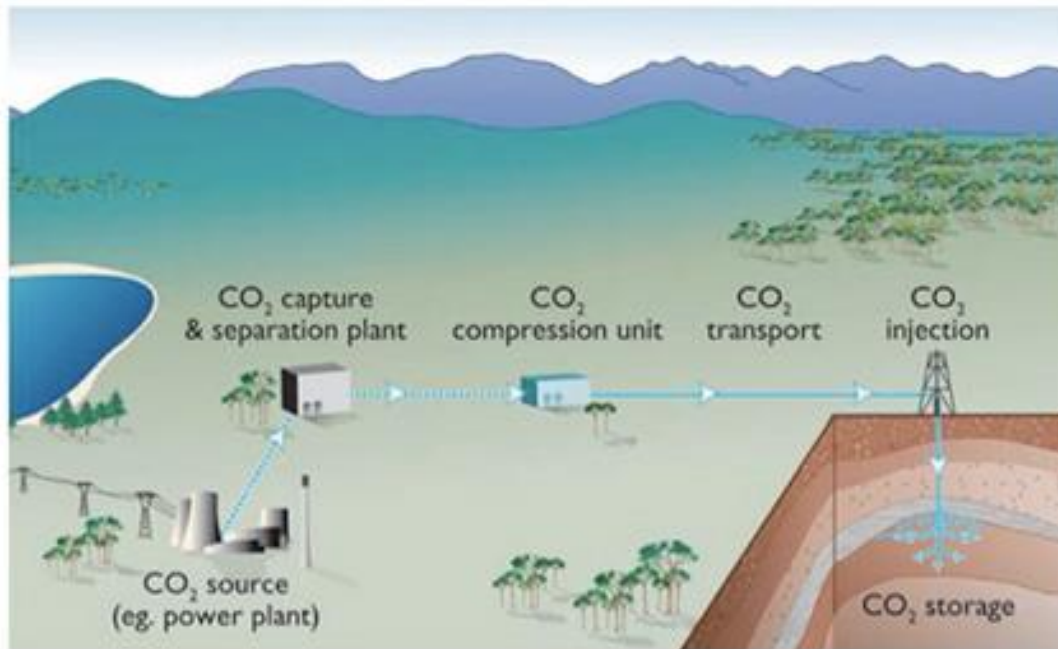


A²¹

CO₂ storage

- The capture and storage of CO₂ in deep geological formations is one of the proposed solutions to reduce CO₂ emissions to the atmosphere.

CARBON CAPTURE AND STORAGE (CCS) PROCESS



Source: Cooperative Research Center for Greenhouse Gas Technologies (CO₂CRC)

CO₂ storage

- CO₂ is injected as a supercritical fluid deep below a confining geological formation that prevents its return to the atmosphere.

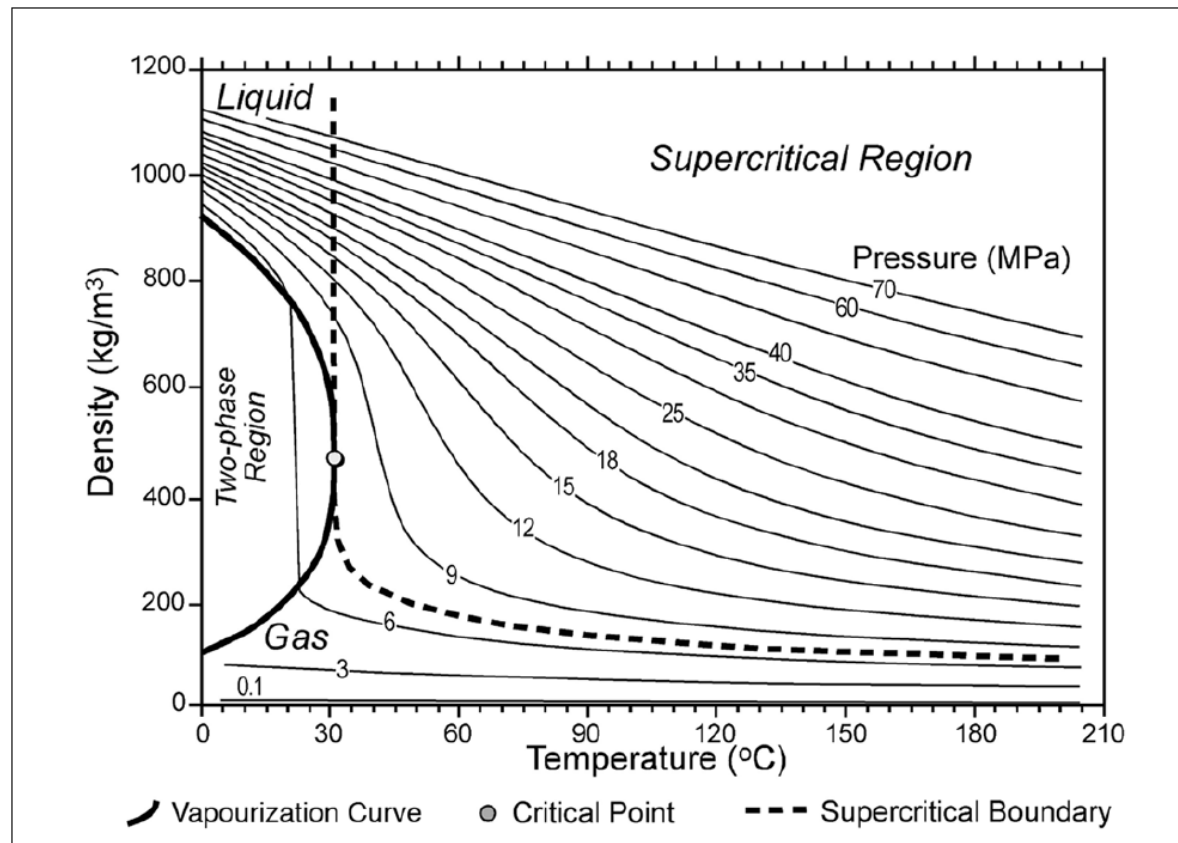
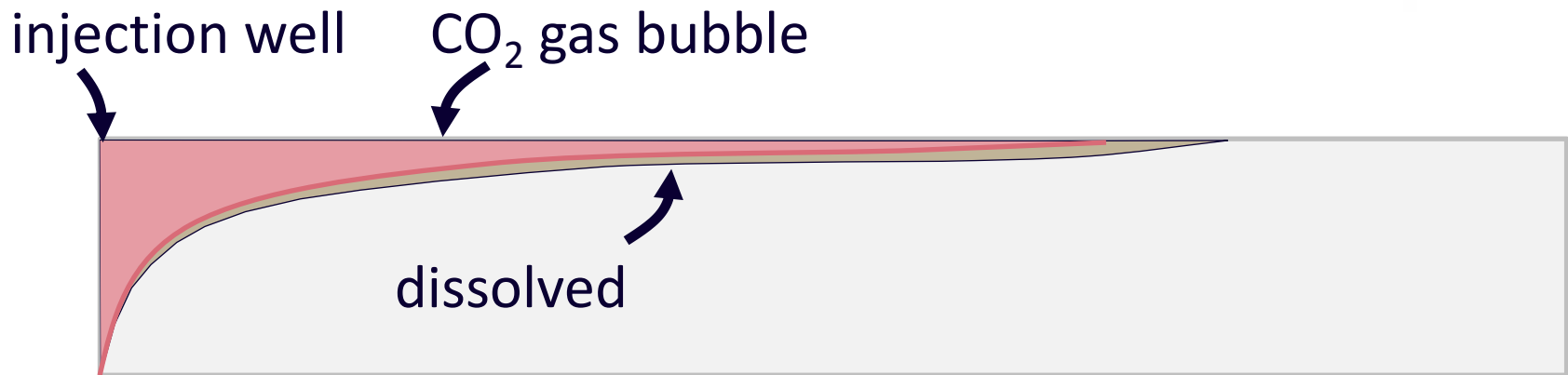


Figure AI.2 Variation of CO₂ density as a function of temperature and pressure (Bachu, 2003).

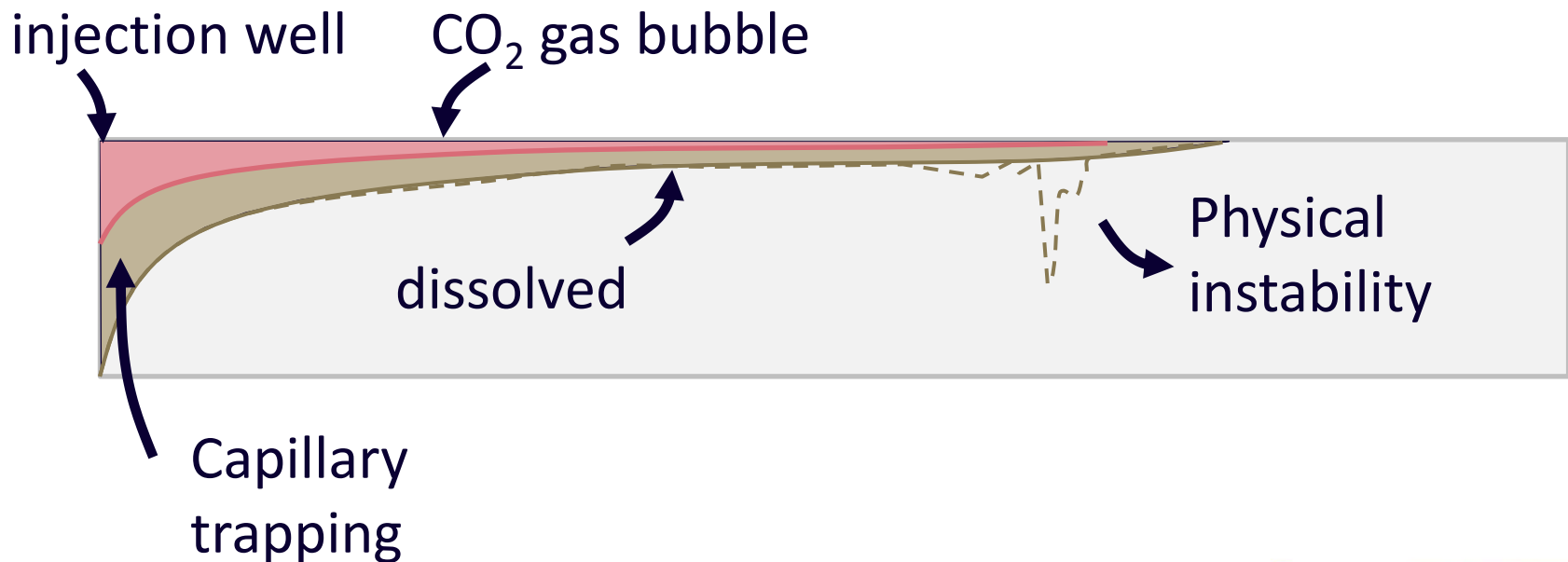
CO₂ storage

- Four trapping mechanisms are expected, which are of increasing importance through time (1) structural, (2) residual saturation, (3) dissolution, and (4) mineral trapping.



CO₂ storage

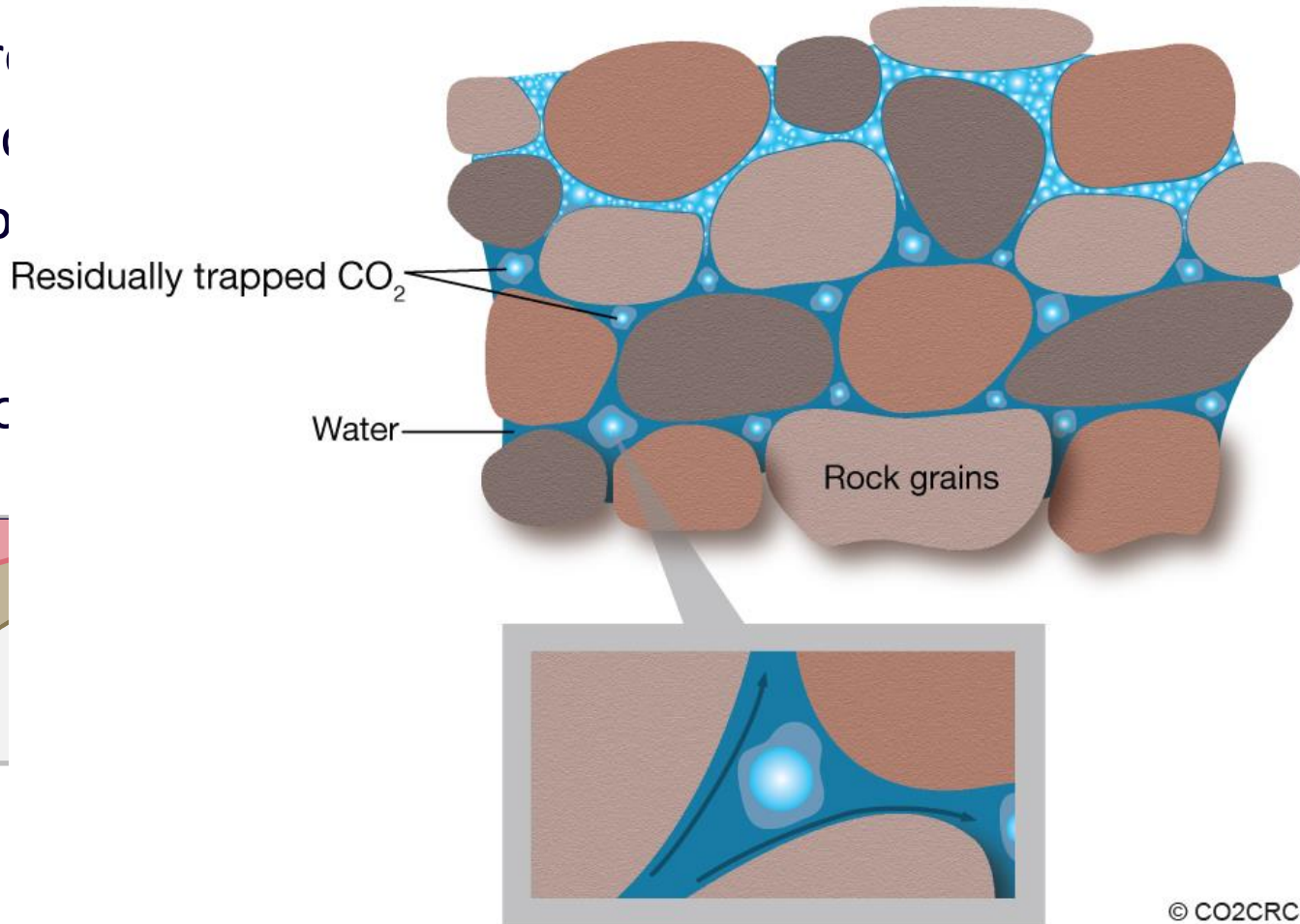
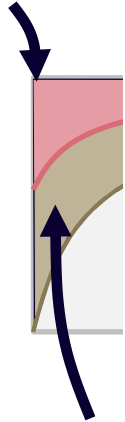
- Four trapping mechanisms are expected, which are of increasing importance through time (1) structural, (2) residual saturation, (3) dissolution, and (4) mineral trapping.



CO₂ storage

- Four
incre
resid
trap

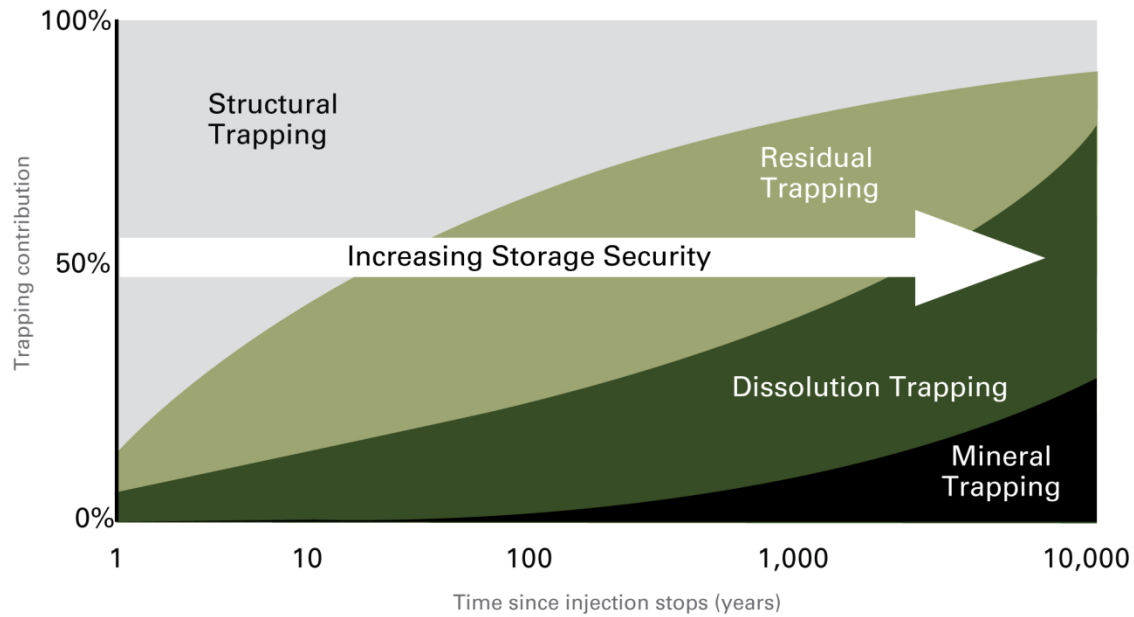
injectio



Source: Cooperative Research Centre for Greenhouse Gas Technologies (CO2CRC)

CO2 storage

- The prediction of the mass of CO₂ stored through time in storage systems is an essential parameter in the pre-injection assessment of a geological storage. For safety reasons, it is relevant to know the mass of CO₂ trapped under these different trapping mechanisms.



Source: Intergovernmental Panel on Climate Change, 2008

Objective

- Identify and quantify the different Co₂ trapping mechanisms in a saline aquifer

Mathematical description

mass species conservation

$$\partial_t(\phi s_\alpha \rho_\alpha m_\alpha^\kappa M^\kappa) = -\nabla(\mathbf{q}_\alpha \rho_\alpha m_\alpha^\kappa M^\kappa - \phi s_\alpha \rho_\alpha \mathbf{D}_\alpha \nabla(m_\alpha^\kappa M^\kappa)) + Q_\alpha^\kappa + T_\alpha^\kappa$$

$$\alpha = l, g \quad \kappa = CO_2, w$$

Darcy's law

$$\mathbf{q}_\alpha = -\frac{k k_{r,\alpha}}{\mu_\alpha} (\nabla p_\alpha - \rho_\alpha \mathbf{g})$$

Mathematical description

[1] Brooks, R. H. & Corey, A. T., 1964. Hydraulic properties of porous media. Hydrology Papers, Colorado State University, Issue March.

constitutive relations

retention curve

sum of phase saturations

$$s_g + s_l = 1$$

pressure equilibria

$$p_c = p_g - p_l$$

effective saturation

$$s_e = \frac{s_l - s_l^r}{1 - s_l^r - s_g^r} \quad [1]$$

capillary pressure

$$p_c = p_t s_e^{-1/\omega} \quad [1]$$

relative liquid permeability

$$k_l^r = s_e^{\frac{2+3\omega}{\omega}} \quad [1]$$

relative gas permeability

$$k_g^r = (1 - s_e)^2 \left(1 - s_e^{\frac{2+\omega}{\omega}} \right) \quad [1]$$

Mathematical description

constitutive relations

gas properties

$$\text{volume} \quad V_g = V_g(p_g, T, m_l^{CO_2}, m_s^{NaCl}) \quad [2]$$

$$\text{phase composition} \quad \bar{m}_l^{CO_2} = \bar{m}_l^{CO_2}(p_g, T, V_g, m_s^{NaCl}) \quad [2]$$

$$\text{density} \quad \rho_g = \frac{M^{CO_2}}{V_g} \quad [3]$$

$$\text{viscosity} \quad \mu_g = \mu_g(p_g, T, m_l^{CO_2}, m_s^{NaCl}) \quad [4]$$

$$\text{enthalpy} \quad h_g = h_g(p_g, T, m_l^{CO_2}, m_s^{NaCl}) \quad [5]$$

[2] Spycher, N. & Pruess, K., 2005. CO₂-H₂O mixtures in the geological sequestration of CO₂. II. Partitioning in chloride brines at 12–100°C and up to 600 bar. *Geochimica et Cosmochimica Acta*, 69(13), pp. 3309-3320.

[3] Nickalls, R., 1993. A new approach to solving the cubic: Cardan's solution revealed. *The Mathematical Gazette*, pp. 354-359.

[4] Altunin, V. & Sakhabetdinov, M., 1972. Application of orthogonal expansions to construct a single equation of state for substances on the basis of various experimental data by means of a digital computer (Orthogonal polynomials for computerized construction of equations of state for substances under thermodynamic restrictions). *Teplofizika Vysokikh Temperatur*, Volume 10, pp. 1195-1202.

[5] Redlich, O. & Kwong, J., 1949. On the Thermodynamics of Solutions. V. An Equation of State. Fugacities of Gaseous Solutions. *Chemical Reviews*, 44(1), pp. 233-244.

Mathematical description

constitutive relations

liquid properties

$$\text{density} \quad \rho_l = \rho_l(\rho_b, \rho_{CO_2}) \quad [6]$$

$$\rho_b = \rho_b(p_l, T, m_l^{CO_2}, m_s^{NaCl}) \quad [7]$$

$$\rho_{CO_2} = \rho_b(p_l, T, m_l^{CO_2}, m_s^{NaCl}) \quad [6]$$

$$\text{viscosity} \quad \mu_g = \mu_g(p_l, T, m_l^{CO_2}, m_s^{NaCl}) \quad [8]$$

$$\text{enthalpy} \quad h_g = h_g(p_l, T, m_l^{CO_2}, m_s^{NaCl}) \quad [9]$$

[6] Garcia, J. E., 2001. Density of aqueous solutions of CO₂.

[7] Haas, J., 1976. Physical Properties of the Coexisting Phases and Thermochemical Properties of the H₂O Component in Boiling NaCl Solutions. USGS Bulletin 1421-A, Washington, DC, p. 73.

[8] Phillips, S. L. et al., 1981. A technical databook for geothermal energy utilization. s.l.:Lawrence Berkeley Laboratory, University of California.

[9] Pruess, K., 2005. ECO2N: A TOUGH2 fluid property module for mixtures of water, NaCl, and CO₂. Lawrence Berkeley National Laboratory Report LBNL-57592, Berkeley, CA.

Formulation used

In this work it will be assumed that water miscibility in gas phase is negligible ($m_g^w = 0$). This is quite reasonable since water dissolution is on the order of tan per mil (Spycher & Pruess, 2005). These restricts the system Eq.[1] to three equations.

For the derivation of the equations notice the following relationships:

$$\sum_{c=CO_2,w} M^c m_\alpha^c = 1$$

$$\sum_{\alpha=l,g} T_\alpha^c = 0$$

$$\sum_{c=CO_2,w} Q_\alpha^c = Q_\alpha$$

Formulation used

The linear combination of the three equations done is the following. A total mass conservation

Eq.[a] is obtained by summing over all the phases and components.

$$\partial_t(\phi s_l \rho_l + \phi s_g \rho_g) = -\nabla(\mathbf{q}_l \rho_l + \mathbf{q}_g \rho_g) + Q_g + Q_l \quad [a]$$

A CO₂ equation mass conservation Eq.[6b] is obtained by summing the Co₂ chemical component equations over the two phases.

$$\begin{aligned} \partial_t(\phi s_l \rho_l m_l^{CO_2} M^{CO_2} + \phi s_g \rho_g) = & -\nabla(\mathbf{q}_l \rho_l m_l^{CO_2} M^{CO_2} + \mathbf{q}_g \rho_g - \rho_l \mathbf{D}_l \nabla(m_l^{CO_2} M^{CO_2})) \\ & + Q_g^{CO_2} + Q_l \end{aligned} \quad [b]$$

Finally, subtracting the equation Eq.[6a] times $m_l^{CO_2} M^{CO_2}$ to the liquid-CO₂ equation we find Eq.[6c]:

$$\begin{aligned} \phi s_l \rho_l \partial_t(m_l^{CO_2} M^{CO_2}) - m_l^{CO_2} M^{CO_2} \partial_t(\phi s_g \rho_g) = & \\ -\mathbf{q}_l \rho_l \nabla(m_l^{CO_2} M^{CO_2}) + m_l^{CO_2,*} M^{CO_2} \nabla(\mathbf{q}_g \rho_g) + \nabla(\rho_l \mathbf{D}_l \nabla(m_l^{CO_2} M^{CO_2})) & \\ -\mathbf{q}_l \rho_l M^{CO_2} (m_l^{CO_2} - m_l^{CO_2,*}) + Q_l^{CO_2} + T_l^{CO_2} & \end{aligned} \quad [c]$$

where $m_l^{CO_2,*}$ is the prescribed concentration of the inflow fluid in the boundaries and $m_l^{CO_2,*} = m_l^{CO_2}$ in the interior domain.

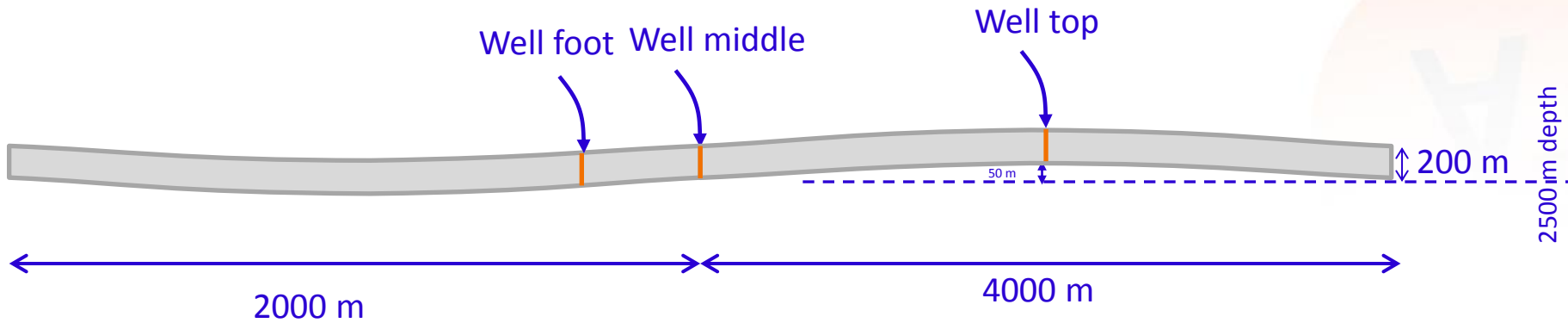
Formulation used

The unknowns for Eq.a, Eq.b, Eq.c chosen are $p_l, S_g, m_l^{CO_2}$ respectively. A conditional kinetic interphase mass transfer is considered.

$$c_1 = \begin{cases} \text{if } (S_g > S_{r,g}), & 1 \\ \text{if } (S_g \leq S_{r,g}), & 0 \end{cases} \qquad c_2 = \begin{cases} \text{if } (m_l^{CO_2} > \bar{m}_l^{CO_2}), & 0 \\ \text{if } (m_l^{CO_2} \leq \bar{m}_l^{CO_2}), & 1 \end{cases}$$

$$T_l^{CO_2} = \phi S_l \rho_l k_{kin} \left(c_1 (m_l^{CO_2} - \bar{m}_l^{CO_2}) + (1 - c_1) c_2 (m_l^{CO_2} - \bar{m}_l^{CO_2}) \right)$$

2D synthetic dome problem



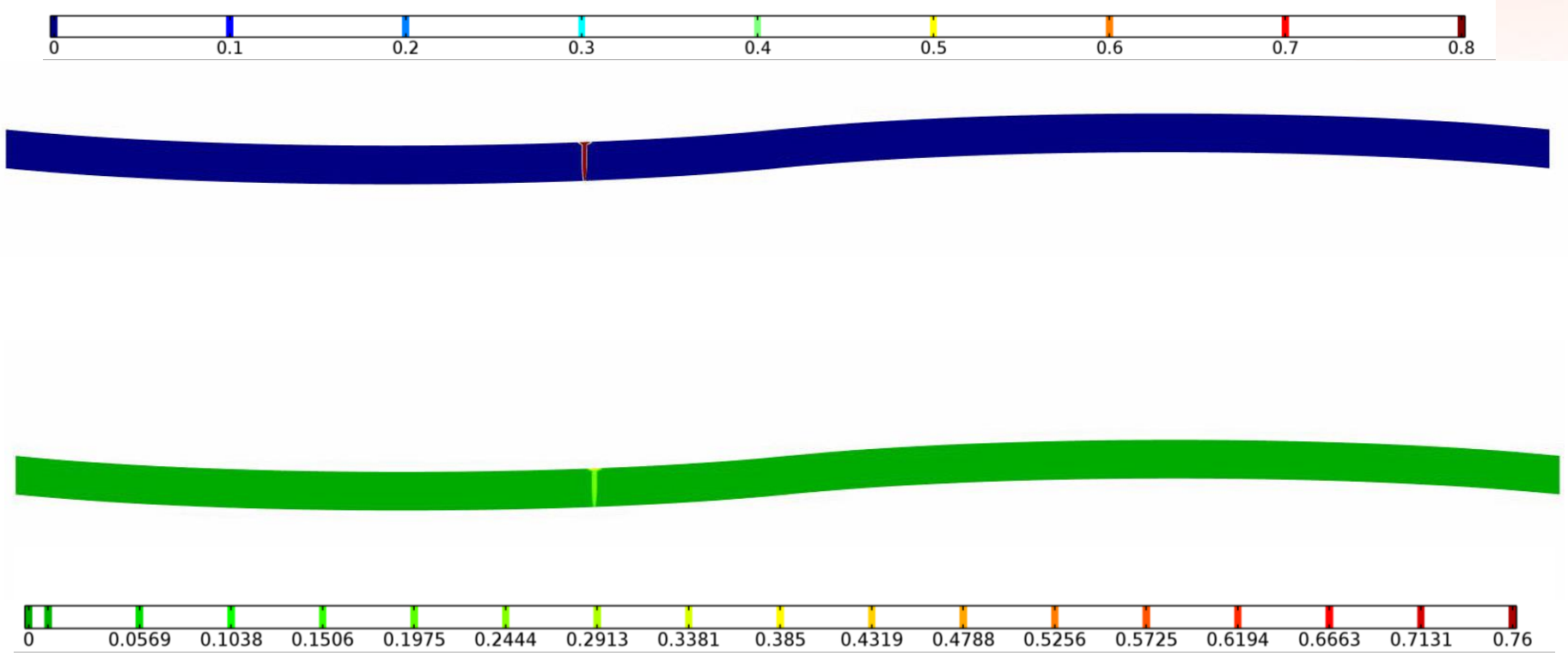
Pumping rate

$$Q_g^{CO_2} = 0.3 \text{ (kg} \cdot \text{s}^{-1}\text{) (during 180 days)}$$

ϕ	0.15	($m^3 \cdot m^{-3}$)
$d_l = d_m$	40	(m)
κ	1e-11	(m^2)
p_t	1e5	(Pa)
ω	2	(-)
s_i^r	0.05	($m^3 \cdot m^{-3}$)
s_g^r	0.1	($m^3 \cdot m^{-3}$)
m_s^{NaCl}	1	($mol \cdot kg^{-1}$)

Results (well foot)

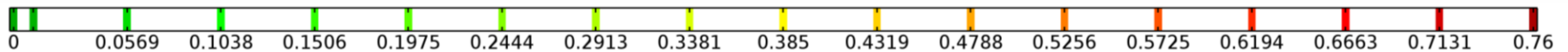
Co2 molality on liquid



Gas saturation

Results (well middle)

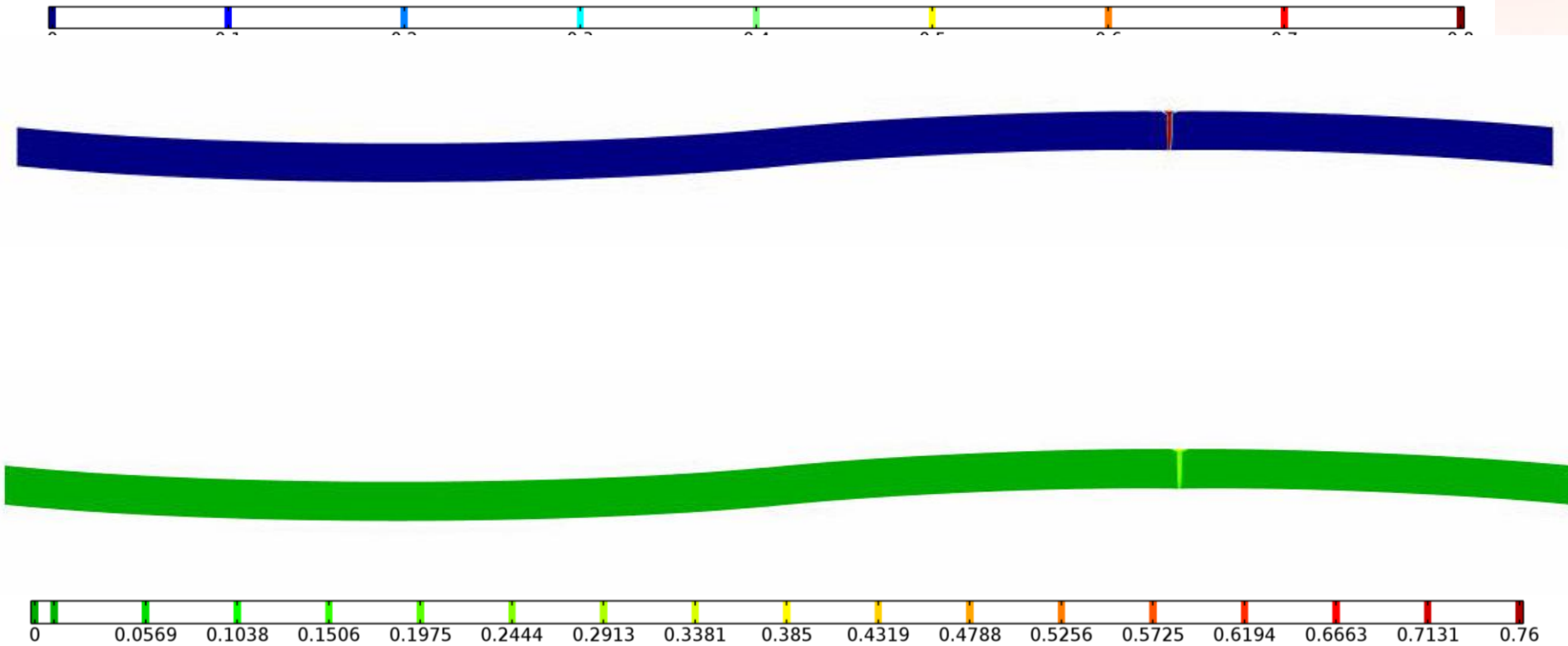
Co2 molality on liquid



Gas saturation

Results (well top)

Co2 molality on liquid



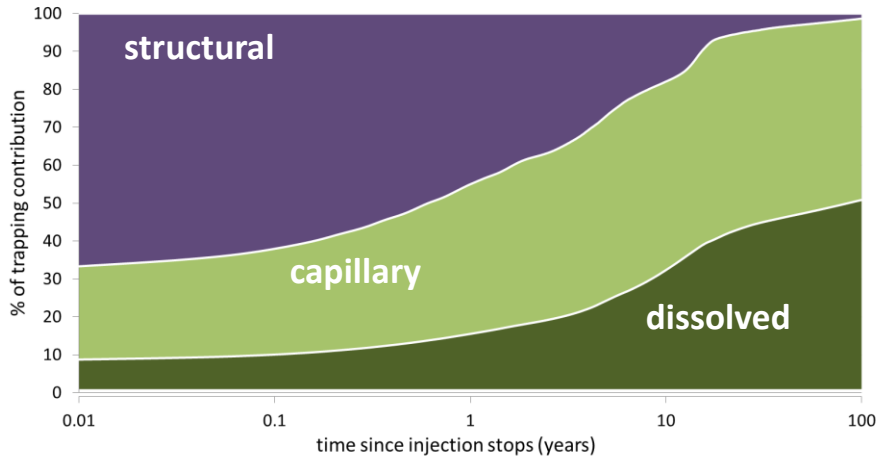
Gas saturation



Results

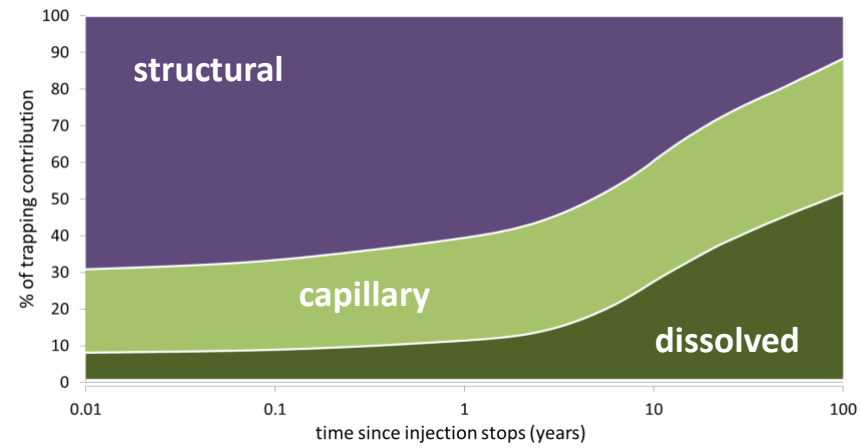
foot

Computed CO₂ trapping evolution



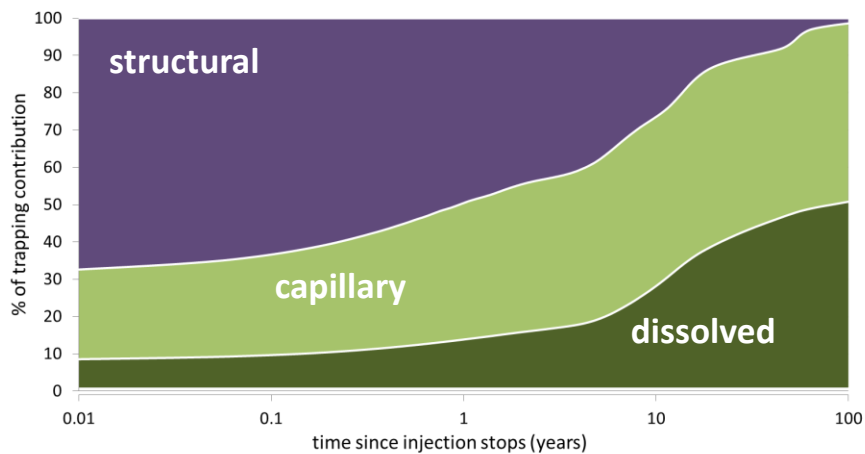
top

Computed CO₂ trapping evolution



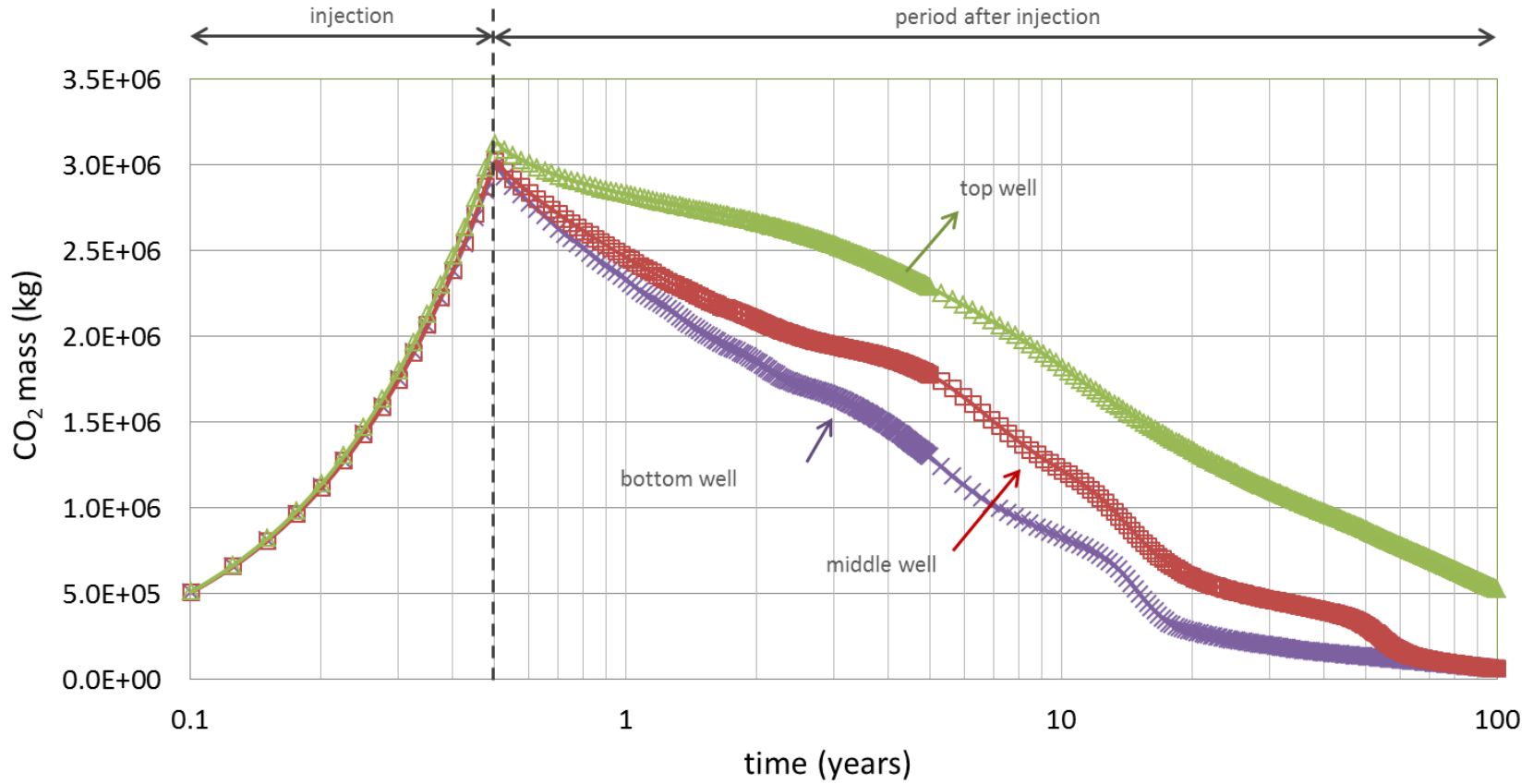
middle

Computed CO₂ trapping evolution



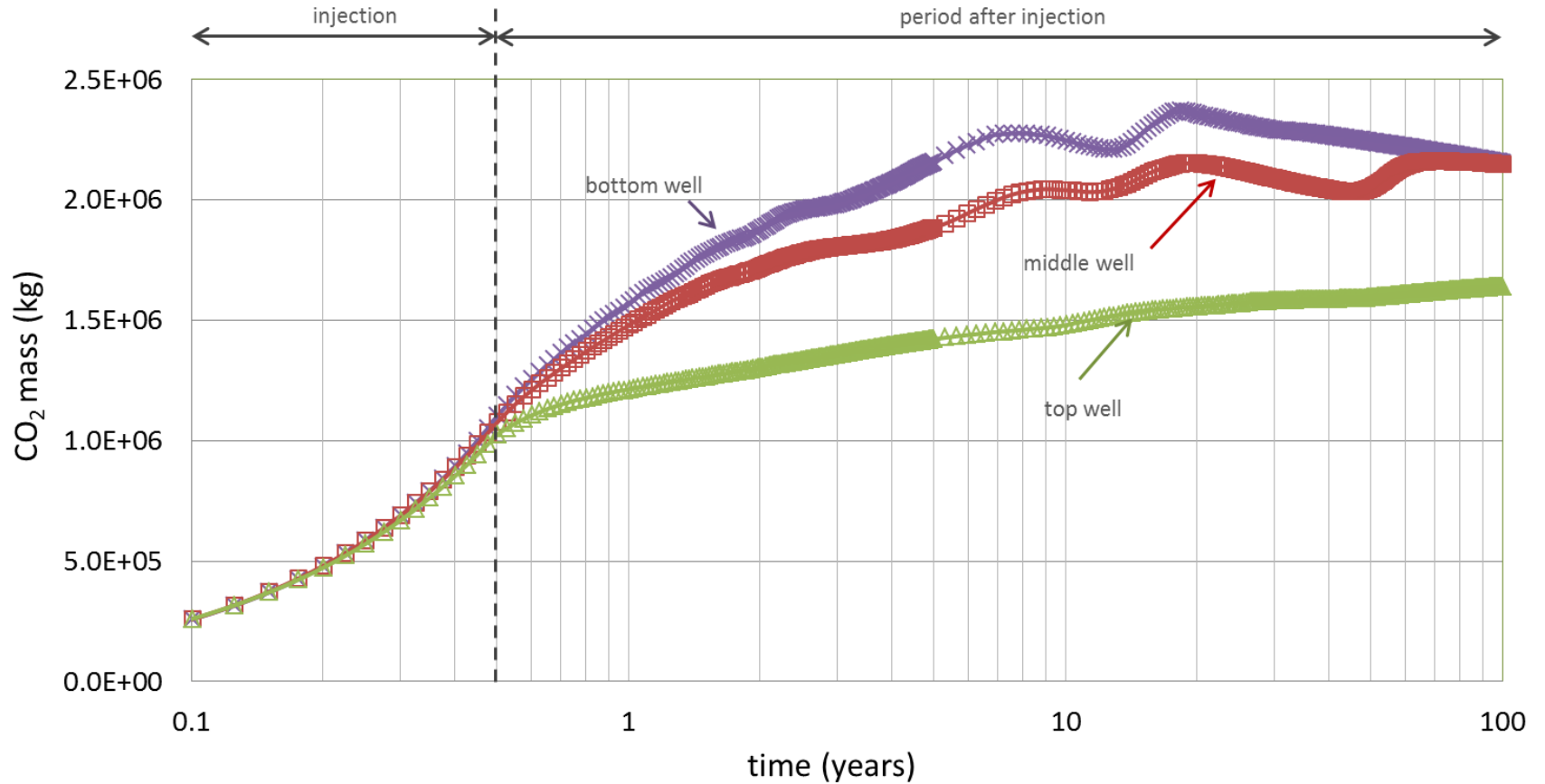
Results

Computed CO₂ free phase



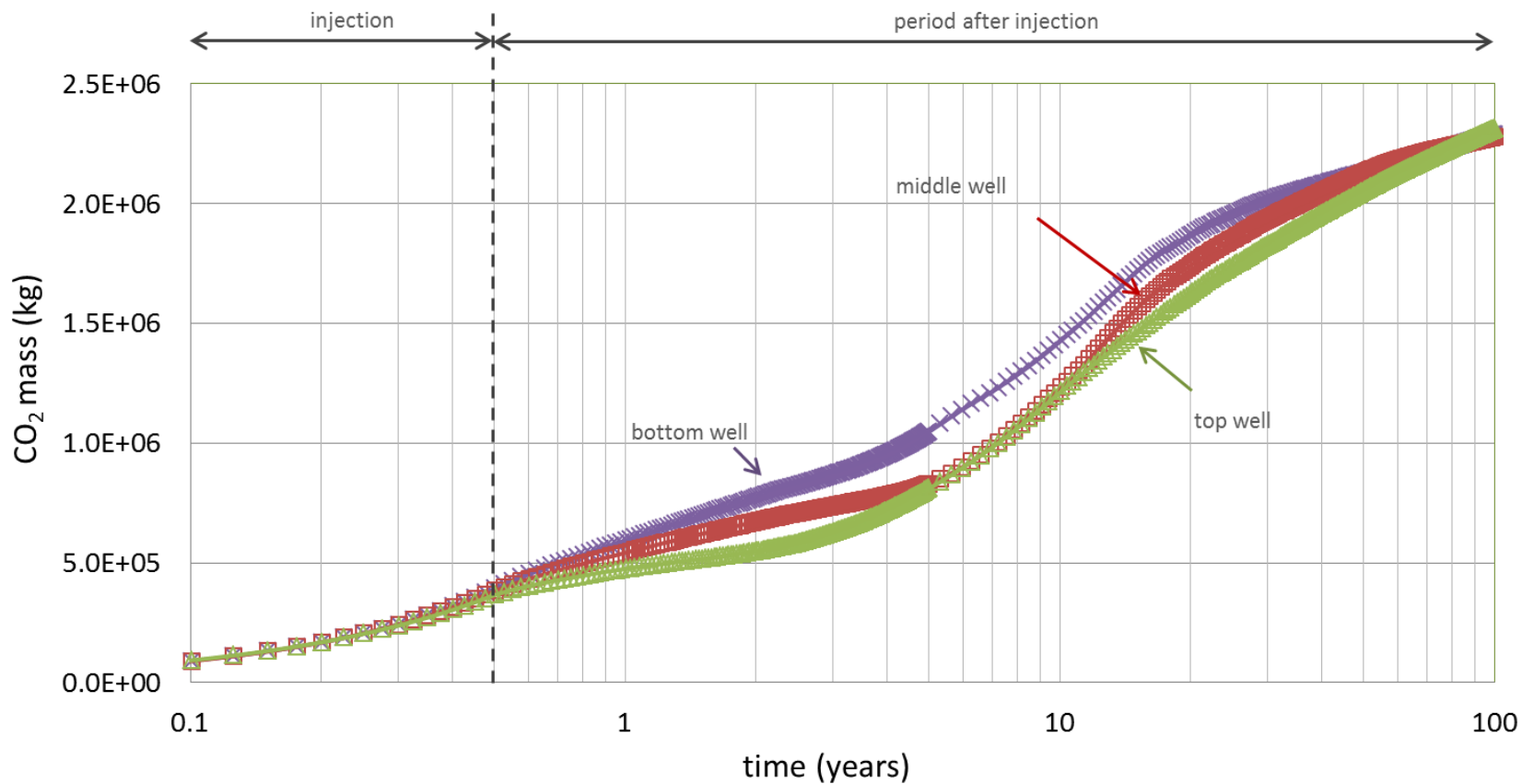
Results

Computed CO₂ trapped by capillarity



Results

Computed CO₂ dissolved in liquid phase



Conclusions

- Expected Co₂ storage systems can be reproduced in a model
- Quantification of this systems is numerically feasible
- The position of the well in a synclinal formation affects the trapping mechanisms.

AMPHOS²¹

SCIENTIFIC AND STRATEGIC ENVIRONMENTAL CONSULTING

ESPAÑA

AMPHOS 21 CONSULTING, S.L.

Paseo de García Faria, 49-51

08019 BARCELONA

Tel.: +34 93 583 05 00; Fax : +34 93 307 59 28

CHILE

AMPHOS 21 CONSULTING CHILE Ltda.

San Sebastián 2839, of. 701-A

Las Condes, 7550180 SANTIAGO DE CHILE

Tel.: +56 2 7991630

PERÚ

AMPHOS 21 CONSULTING PERU, S.A.C.

Av. del Parque Sur 661, San Borja

Lima 41

Tel.: +511 592-1275

FRANCE

AMPHOS 21 CONSULTING FRANCE SARL

14 Avenue de l'Opéra

75001 PARIS

Tel.: +33 1 46946917

