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# Non-invasive Breast Cancer Imaging Using Novel Estrogen Conjugates NIR Fluorescent Dye

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# Diffuse Optical Tomography(DOT) in cancer detection

- Diffuse Optical Tomography ? NIR?
- Why not MIR, PET, CT, x ray mammogram?
- Add on existing modalities.
- Non-invasive, Inexpensive, Low power, Portable, Resolution
- Tracking cancer spread.



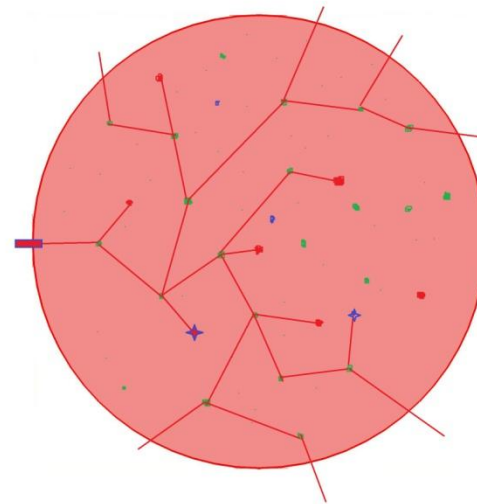
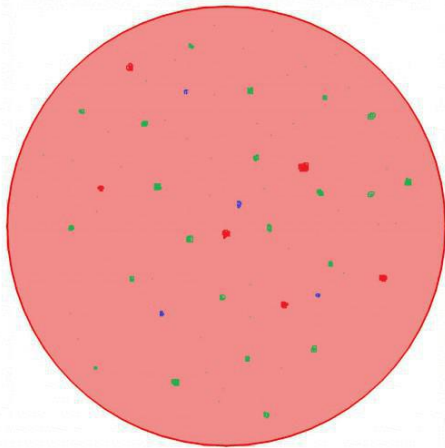
# Tissue interrogation using laser

- P1 Approximation of Radiative Transport Equation

$$-\nabla \cdot (D_x \nabla \phi_x(r)) + \left[ \mu_{axi} + \mu_{axf} + \frac{i\omega}{c} \right] \phi_x(r) = -\Theta_s \delta(r - r_s) \quad D_x = \frac{1}{3(\mu_{axi} + \mu_{axf} + \mu'_{sx})}$$

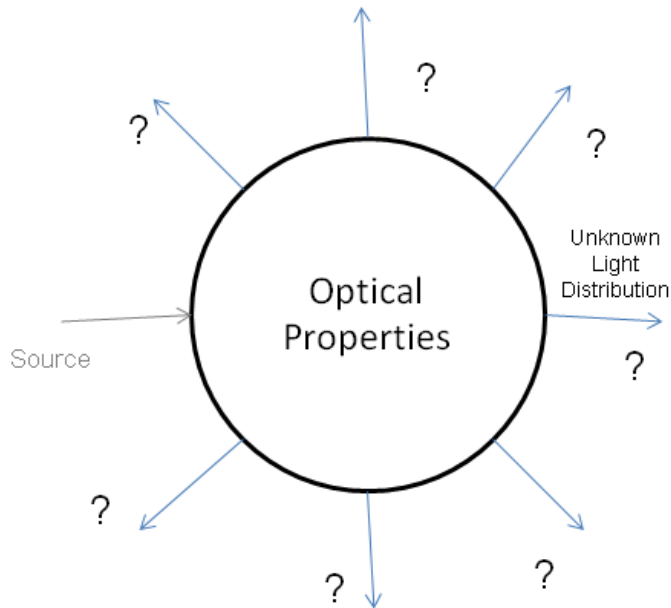
- Robin Boundary condition

$$\mathbf{n} \cdot [2A_x D_x \nabla \phi_x(r)] + \phi_x(r) = 0 \quad \forall r \in \partial\Omega$$

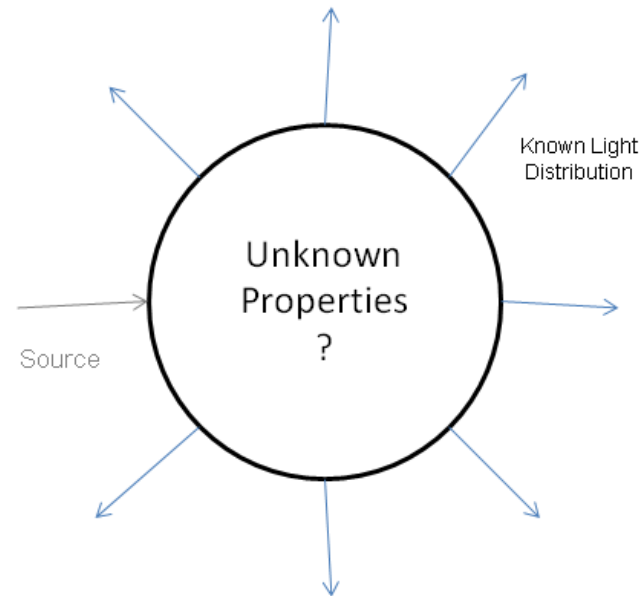


# Problems in DOT

Forward problem



Inverse problem



Normal tissue  $\mu_a$  0.005 to 0.02 mm<sup>-1</sup>  
 $\mu_s'$  2 to 15 mm

# Inverse problem in DOT

- Start with uniform optical properties
- Jacobian – using adjoint method

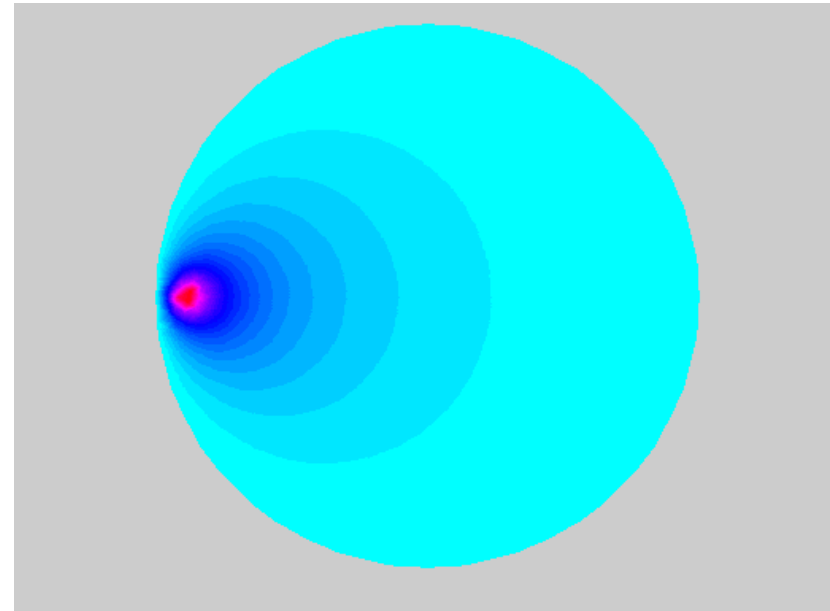
$$\frac{\partial \phi^c}{\partial \mu}$$

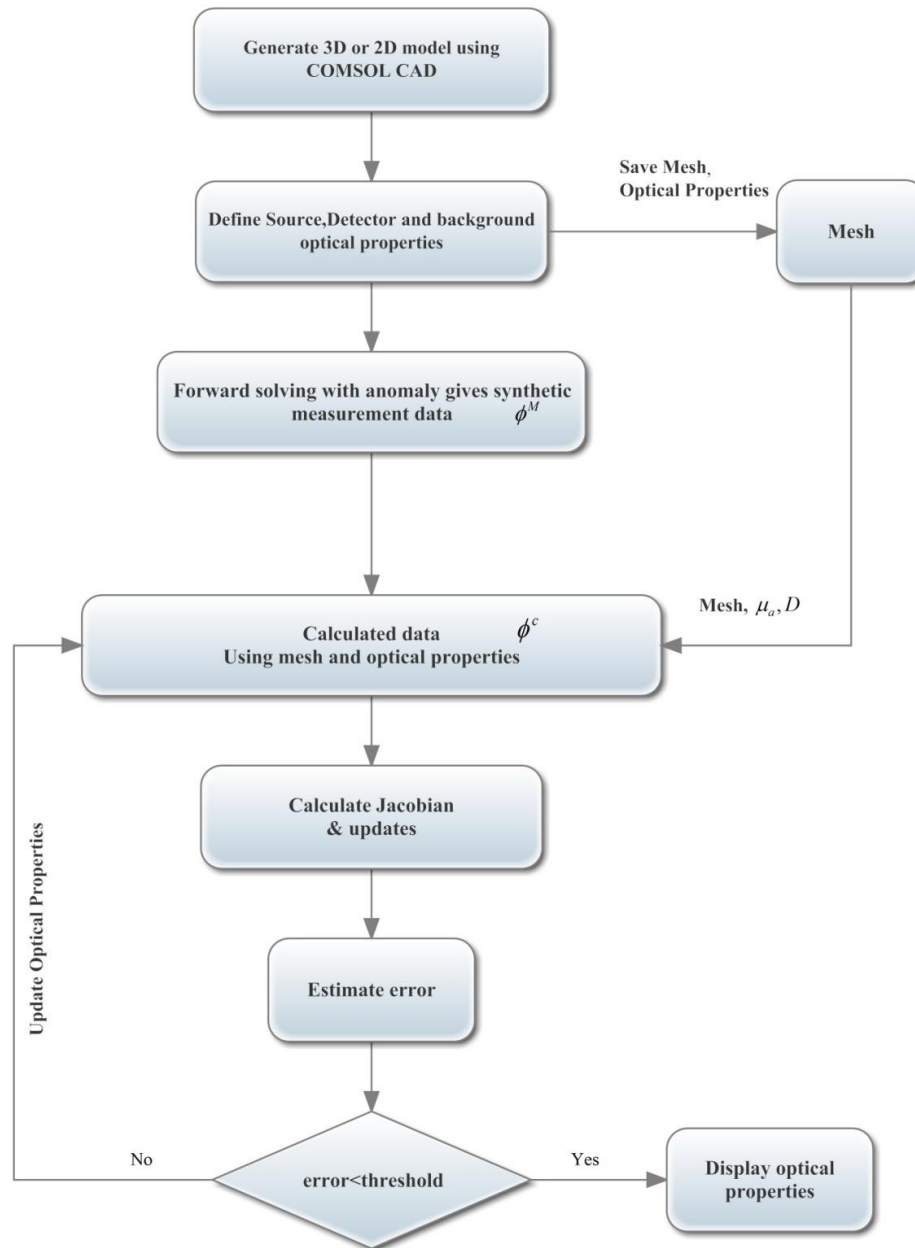
- Optical Property update  
Levenberg-Marquardt

$$\partial \mu = (J^T J + \bar{\lambda} I)^{-1} J^T \partial \phi$$

- Tikhonov minimization of error

$$\chi^2 = \min_{\mu} \left\{ \sum_{i=1}^M (\phi_i^M - \phi_i^C)^2 \right\}$$





# Target specific fluorescent dye

- Contrast agents – ICG
- Estrogen receptor
- $\lambda_{ex} = 754nm$  &  $\lambda_{em} = 787nm$
- Early cancer detection & tracking

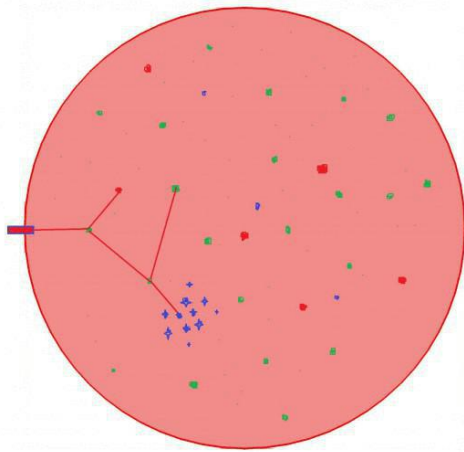
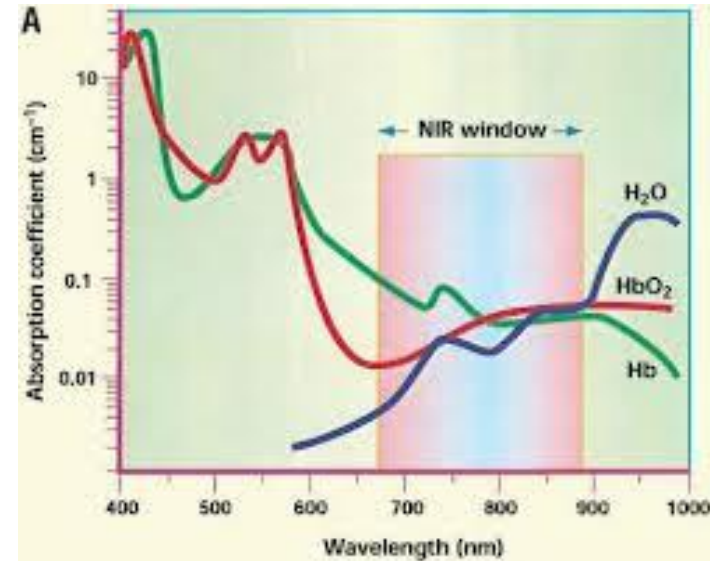
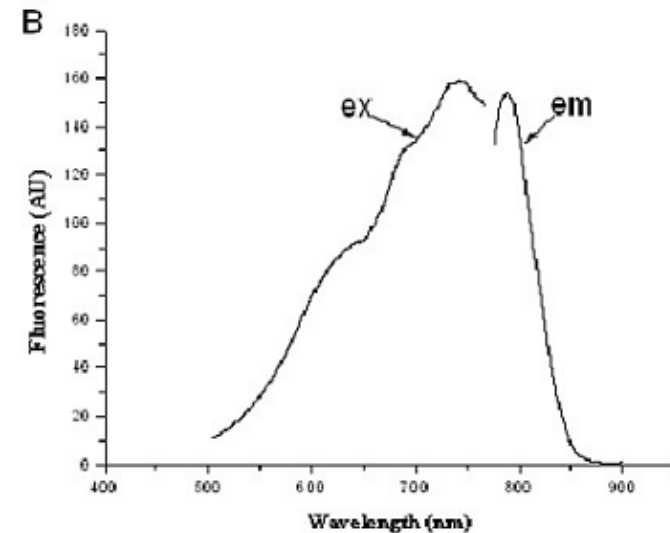


Image courtesy: National Cancer Institute



# Modeling fluorescent dye

- Forward solving

>>Excitation

$$-\nabla \cdot (D_x \nabla \phi_x(r)) + \left[ \mu_{axi} + \mu_{axf} + \frac{i\omega}{c} \right] \phi_x(r) = -\Theta_s \delta(r - r_s)$$

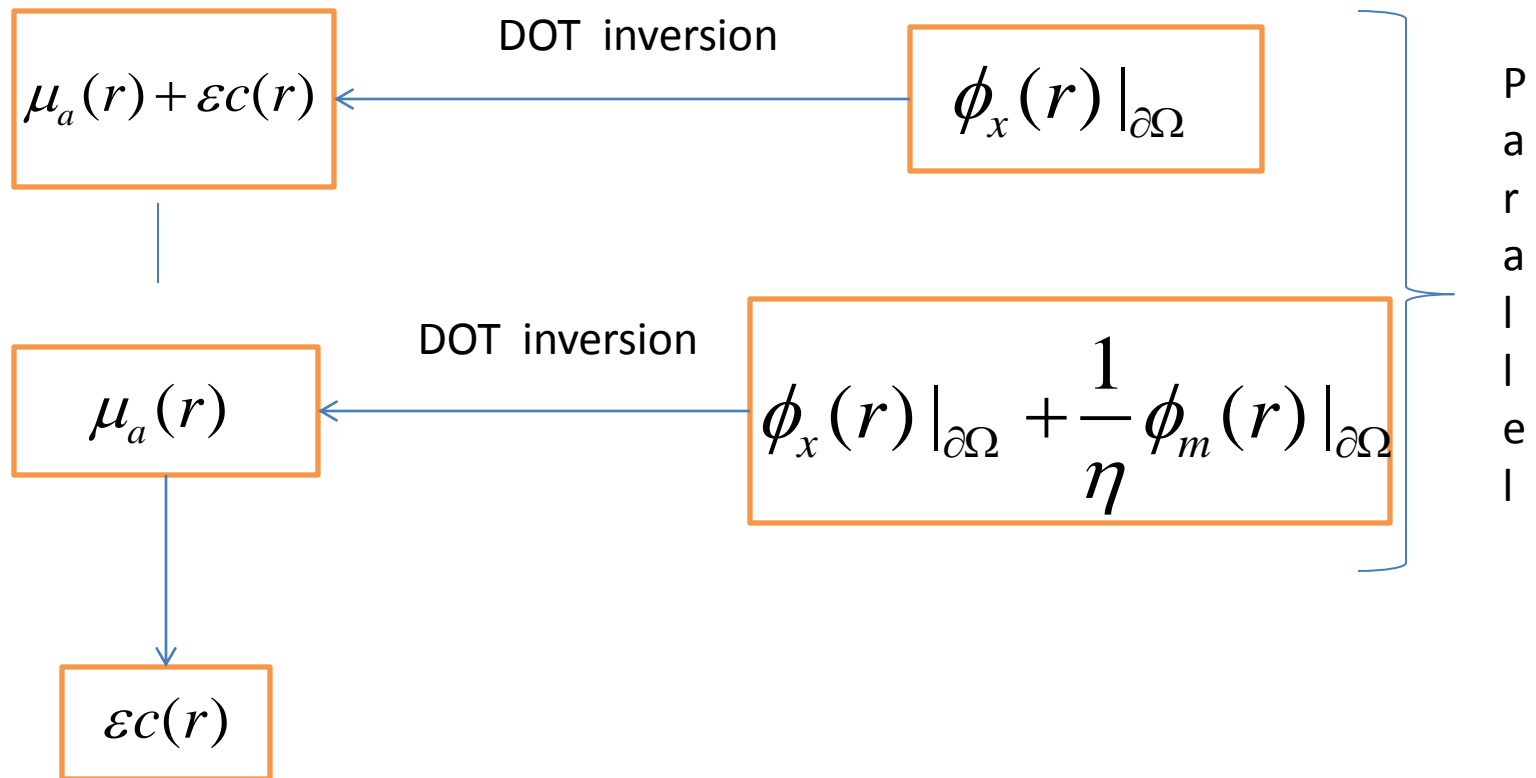
>>Emission

$$-\nabla \cdot (D_m \nabla \phi_m(r)) + \left[ \mu_{ami} + \frac{i\omega}{c} \right] \phi_m(r) = -\frac{\phi_x(r) \eta \mu_{axf}}{1 - i\omega\tau}$$

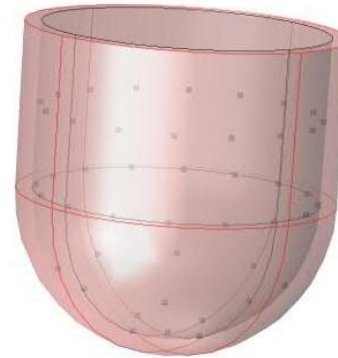
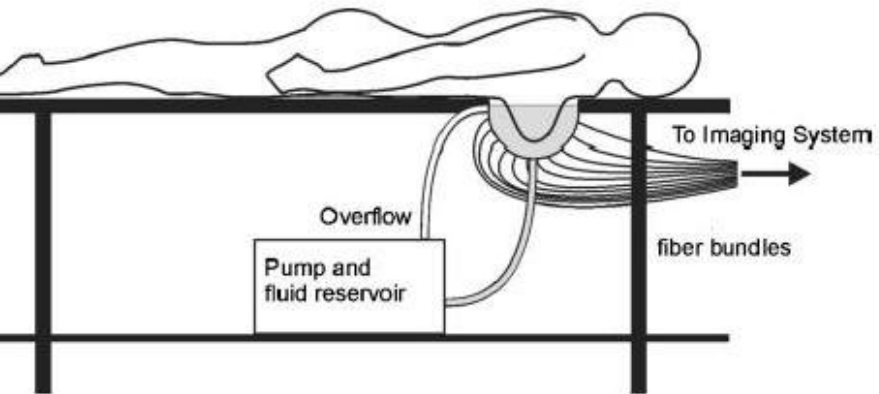
- Robin boundary condition
- Separating coupled equations



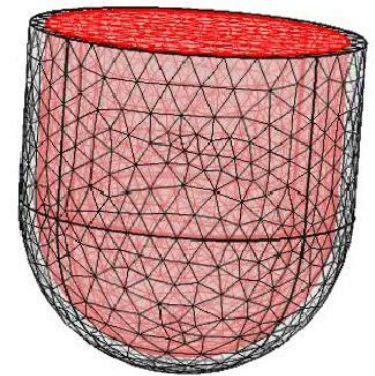
# Fluorescent reconstruction



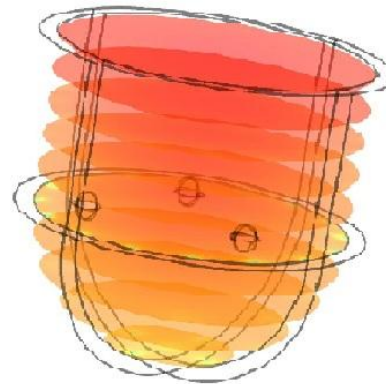
# Results



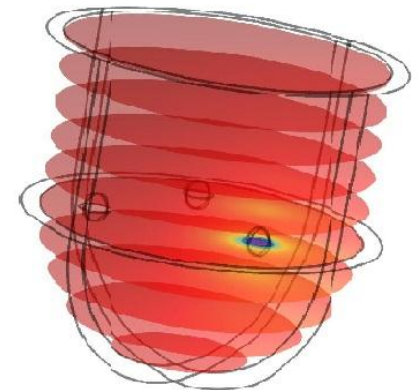
(a)



(b)

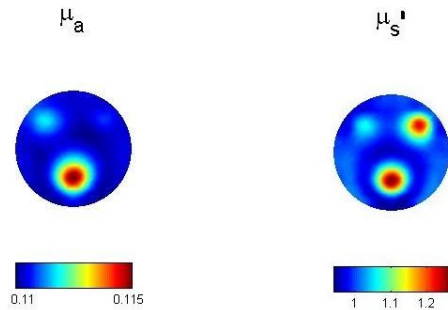


(c)

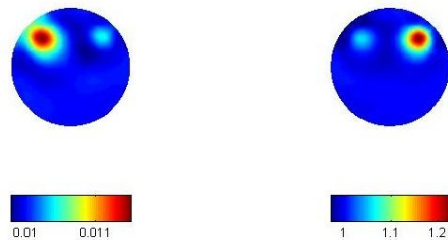


(d)

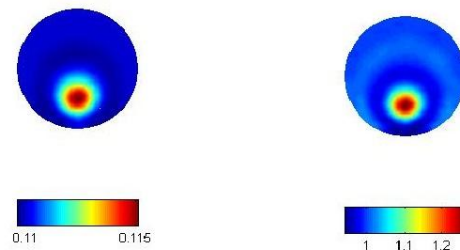
# Results



(a) Optical properties at excitation wavelength



(b) Optical properties at emission wavelength



(c) Reconstructed optical properties of fluorescent dye

Domain	$\mu_a$ (mm-1)	$\mu'_s$ (mm-1)
Background	0.01	1
Absorber	0.02	1
Scatterer	0.01	2
Dye	0.115	2

$$E = \frac{1}{N} \| F(x) - y \|^2$$

Parameter	Error Function ( $E$ )
Amplitude	9.3705e-07
Phase	2.4401e-03

Parameter	MSE
$\mu_a$	0.0024
$\mu'_s$	0.0010

# Reference

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3. Iven J, Gargi V, Kodand D,Uday D,"Non invasive imaging of breast cancer: Synthesis and study of novel near-infrared fluorescent estrogen conjugate", *Proc.SPIE*, 5693, p.521-527, (2005).
4. Shubhadeep B, Iven J, Early detection of Breast Cancer:A molecular optical imaging approach using novel estrogen conjugate fluorescent dye, *Proc.SPIE*,7896, 1F1-1F15,(2012)
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6. Ralf B, Jorg P, Wolfhard S, Independent modeling of fluorescence excitation and emission with the finite element method, *OSA, BioMed*,(2004)
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8. Tara D, S R. Arridge, Time-resolved optical mammography using a liquid coupled interface, *Journal of Biomedical Optics* , Vol 10,p054011-1- 10(2005)
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# More details...

Inverse solving

Tikhonov Minimization

$$\chi^2 = \min_{\mu} \left\{ \sum_{i=1}^M (\phi_i^M - \phi_i^C)^2 \right\}$$

$$\frac{\partial \chi^2}{\partial \mu} = 0$$

$$\left( \frac{\partial \phi^C}{\partial \mu} \right)^2 (\phi^M - \phi^C) = 0$$

Jacobian  $\frac{\partial \phi^C}{\partial \mu}$

LM iterative equation

$$\partial \mu = (J^T J + \bar{\lambda} I)^{-1} J^T \partial \phi$$

# More details...

$$J = \begin{bmatrix}
 \frac{\delta \ln I_1}{\delta \kappa_1} & \frac{\delta \ln I_1}{\delta \kappa_2} & \dots & \frac{\delta \ln I_1}{\delta \kappa_{NN}}; & \frac{\delta \ln I_1}{\delta \mu_{a1}} & \frac{\delta \ln I_1}{\delta \mu_{a2}} & \dots & \frac{\delta \ln I_1}{\delta \mu_{aNN}} \\
 \frac{\delta \theta_1}{\delta \kappa_1} & \frac{\delta \theta_1}{\delta \kappa_2} & \dots & \frac{\delta \theta_1}{\delta \kappa_{NN}}; & \frac{\delta \theta_1}{\delta \mu_{a1}} & \frac{\delta \theta_1}{\delta \mu_{a2}} & \dots & \frac{\delta \theta_1}{\delta \mu_{aNN}} \\
 \frac{\delta \ln I_2}{\delta \kappa_1} & \frac{\delta \ln I_2}{\delta \kappa_2} & \dots & \frac{\delta \ln I_2}{\delta \kappa_{NN}}; & \frac{\delta \ln I_2}{\delta \mu_{a1}} & \frac{\delta \ln I_2}{\delta \mu_{a2}} & \dots & \frac{\delta \ln I_2}{\delta \mu_{aNN}} \\
 \frac{\delta \theta_2}{\delta \kappa_1} & \frac{\delta \theta_2}{\delta \kappa_2} & \dots & \frac{\delta \theta_2}{\delta \kappa_{NN}}; & \frac{\delta \theta_2}{\delta \mu_{a1}} & \frac{\delta \theta_2}{\delta \mu_{a2}} & \dots & \frac{\delta \theta_2}{\delta \mu_{aNN}} \\
 \vdots & \vdots & \ddots & \vdots & \vdots & \vdots & \ddots & \vdots \\
 \frac{\delta \ln I_{NM}}{\delta \kappa_1} & \frac{\delta \ln I_{NM}}{\delta \kappa_2} & \dots & \frac{\delta \ln I_{NM}}{\delta \kappa_{NN}}; & \frac{\delta \ln I_{NM}}{\delta \mu_{a1}} & \frac{\delta \ln I_{NM}}{\delta \mu_{a2}} & \dots & \frac{\delta \ln I_{NM}}{\delta \mu_{aNN}} \\
 \frac{\delta \theta_{NM}}{\delta \kappa_1} & \frac{\delta \theta_{NM}}{\delta \kappa_2} & \dots & \frac{\delta \theta_{NM}}{\delta \kappa_{NN}}; & \frac{\delta \theta_{NM}}{\delta \mu_{a1}} & \frac{\delta \theta_{NM}}{\delta \mu_{a2}} & \dots & \frac{\delta \theta_{NM}}{\delta \mu_{aNN}}
 \end{bmatrix}$$

# More Details...

## FEM formulation

$$\left( K(\kappa) + C\left(\mu_a + \frac{i\omega}{c_m}\right) + \frac{1}{2A}F \right) \Phi = q_0$$

where the matrices  $K(\kappa)$ ,  $C((\mu_a + i\omega/c_m))$  and  $F$  have entries given by

$$K_{ij} = \int_{\Omega} \kappa(r) \nabla u_i(r) \cdot \nabla u_j(r) d^n r$$

$$C_{ij} = \int_{\Omega} \left( \mu_a(r) + \frac{i\omega}{c_m(r)} \right) u_i(r) u_j(r) d^n r$$

$$F_{ij} = \oint_{\partial\Omega} u_i(r) u_j(r) d^{n-1} r$$

and the source vector  $q_0$  has terms

$$q_{0i} = \int_{\Omega} u_i(r) q_0(r) d^n r$$



# More detail...

$$-\nabla \cdot \kappa(r) \nabla \Phi(r, \omega) + \left( \mu_a(r) + \frac{i\omega}{c_m(r)} \right) \Phi(r, \omega) = q_0(r, \omega)$$

$$\kappa = 1/3(\mu_a + \mu'_s)$$

$$\Phi(\xi, \omega) + 2A \hat{\mathbf{n}} \cdot \kappa(\xi) \nabla \Phi(\xi, \omega) = 0$$

$$A = \frac{2/(1 - R_0) - 1 + |\cos \theta_c|^3}{1 - |\cos \theta_c|^2}$$

$$\vartheta_c = \arcsin(n_{\text{AIR}}/n_1)$$

$$R_0 = (n_1/n_{\text{AIR}} - 1)^2 / (n_1/n_{\text{AIR}} + 1)^2$$

# More Detail

$$-\nabla \cdot (D_x \nabla \phi_x(r)) + \left[ \mu_{axi} + \mu_{axf} + \frac{i\omega}{c} \right] \phi_x(r) = -\Theta_s \delta(r - r_s) \quad (1a)$$

$$-\nabla \cdot (D_m \nabla \phi_m(r)) + \left[ \mu_{ami} + \frac{i\omega}{c} \right] \phi_m(r) = -\frac{\phi_x(r) \eta \mu_{axf}}{1 - i\omega\tau} \quad (1b)$$

$$D_x = \frac{1}{3(\mu_{axi} + \mu_{axf} + \mu'_{sx})}$$

$$D_m = \frac{1}{3(\mu_{ami} + \mu'_{sm})}$$

$$\mathbf{n} \cdot [2A_x D_x \nabla \phi_x(r)] + \phi_x(r) = 0 \quad \forall r \in \partial\Omega \quad (2a)$$

$$\mathbf{n} \cdot [2A_m D_m \nabla \phi_m(r)] + \phi_m(r) = 0 \quad \forall r \in \partial\Omega \quad (2b)$$

# More Details...

$$A = \frac{2 / (1 - R_0) - 1 + |\cos(\theta_c)|^3}{1 + |\cos(\theta_c)|^2}$$

$$D_x = D_m = D \quad \mu_{ax} = \mu_{am} = \mu_a$$

$$-\nabla \cdot (D_x \nabla \phi_x(r)) + \left[ \mu_a + \varepsilon_x c(r) + \frac{i\omega}{c} \right] \phi_x(r) = -\Theta_s \delta(r - r_s) \quad (3a)$$

$$-\nabla \cdot (D_m \nabla \phi_m(r)) + \left[ \mu_a + \frac{i\omega}{c} \right] \phi_m(r) = -\frac{\phi_x(r) \eta \varepsilon_x c(r)}{1 - i\omega\tau} \quad (3b)$$

$$\varepsilon_x c(r) \phi_x(r) = \Theta_s \delta(r - r_s) - \left( -\nabla D \nabla + \mu_a(r) + \frac{i\omega}{c} \right) \phi_x(r) \quad (4)$$

# More Details...

$$\left[ -\nabla D \nabla + \mu_a(r) + \frac{i\omega}{c} \right] \left( \frac{1-i\omega\tau}{\eta} \phi_m(r) + \phi_x(r) \right) = \Theta_s \delta(r-r_s) \quad (5)$$

Let  $\frac{1-i\omega\tau}{\eta} \phi_m(r) + \phi_x(r) = \phi_t(r)$

$$\left[ -\nabla D \nabla + \mu_a + \varepsilon_x c(r) + \frac{i\omega}{c} \right] \phi_x(r) = -\Theta_s \delta(r-r_s) \quad (6a)$$

$$\left[ -\nabla D \nabla + \mu_a(r) + \frac{i\omega}{c} \right] \phi_t(r) = \Theta_s \delta(r-r_s) \quad (6b)$$