

## Numerical Simulation of the One-Way Mechanical-Electrochemical Coupling in Structural Supercapacitors

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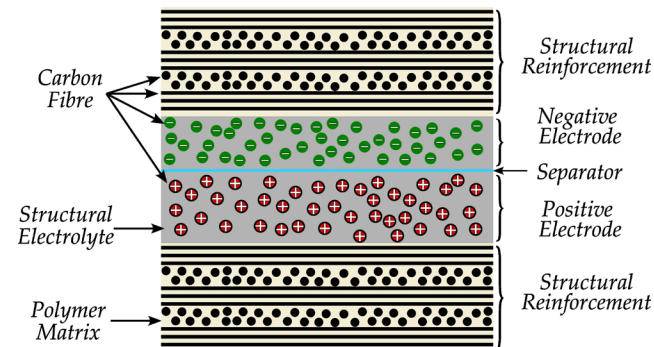
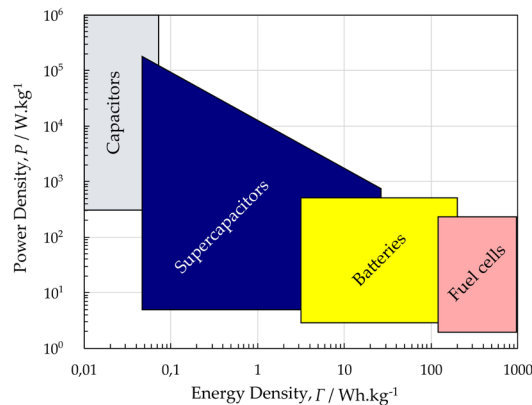
# Multifunctional Energy Storage Composites

- Multifunctional Energy Storage Composite (MESC) carry load and store energy simultaneously.



[D. Peyrow Hedayati, ICCM23 Conf. Proc.]

- Examples: Structural Battery (SB) and Structural Supercapacitor (SSC)



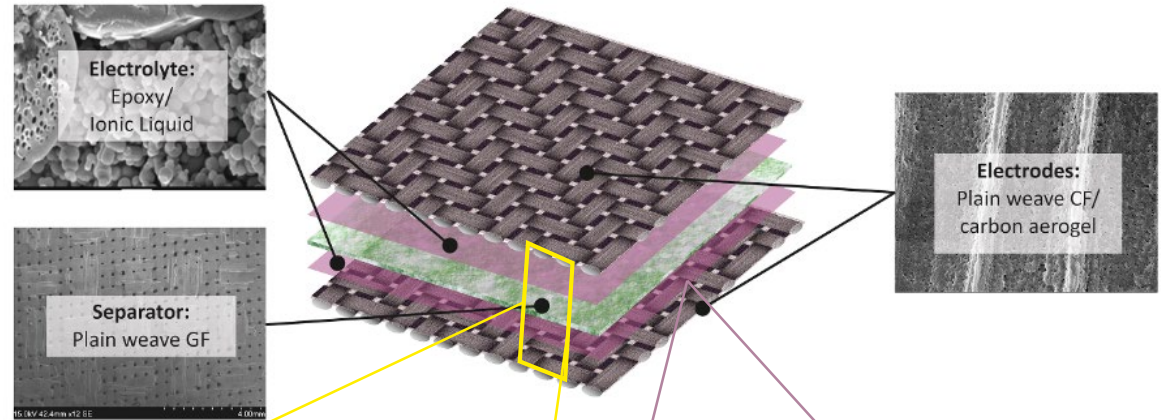
- High power density (SSC) for fast charge/discharge applications

# Structural Supercapacitors

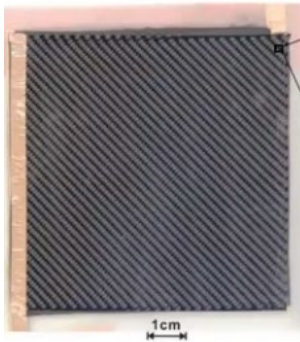
## Architecture

SSC components:

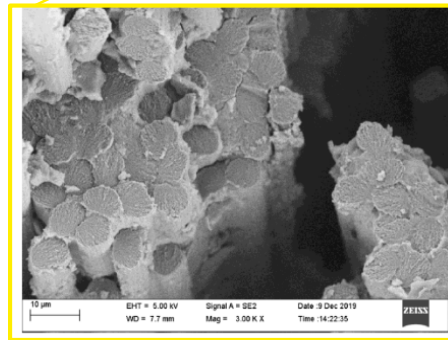
- Electrode (CF)
- Structural Electrolyte
- Separator



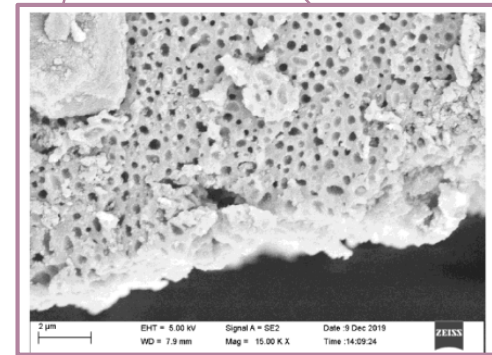
SSC demonstrator



[E. S Greenhalgh (2023, October 6), *Structural power composites - the route to more electric aircraft*]



SSC composite



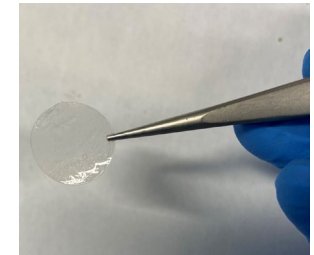
SSC matrix

[M.F. Pernice *et al* 2022 *Multifunct. Mater.* 5 025002]

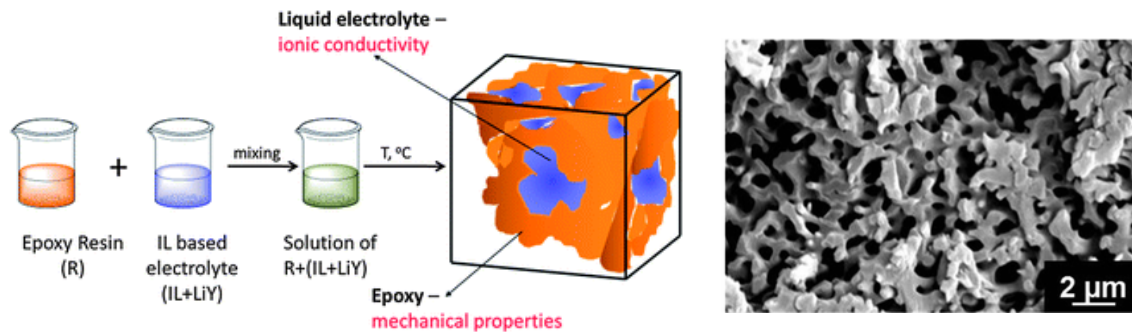
# Structural Electrolytes

- Structural electrolytes: *ionically conductive + high mechanical integrity*
- Gel polymers are typically used but not stiff for structural applications.

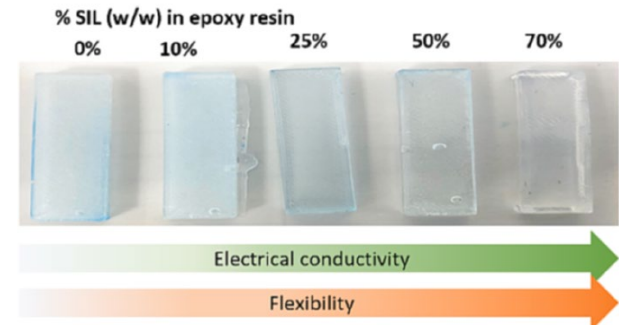
- Novel solution: **bicontinuous porous polymer electrolytes**
  - Porous polymer skeleton: non-conducting and stiff
  - Ionic liquid: ion conductive



[D. Peyrow Hedayati, *Materials* 2023, 16(3), 1232]

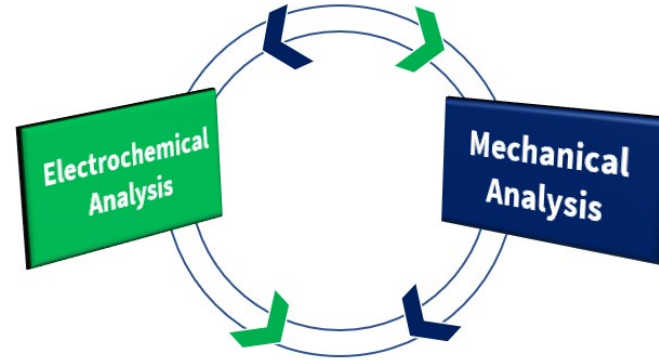


[Shirshova, *J. Mater. Chem. A*, 2013, 1, 15300-15309]



[Dharmasiri, *CEJ*, V.455, P.2, 2023, 140778]

# Motivation and objective

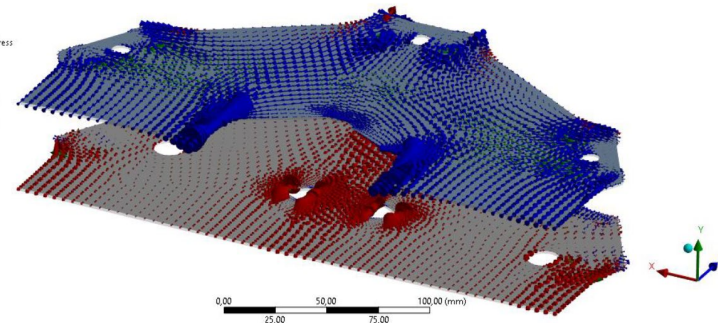


- Multiphysics in a SSC
- SSCs as structural parts need to sustain mechanical loads.



F: Static Structural  
Vector Principal Stress  
Type: Vector Principal Stress  
Unit: MPa  
Time: 1 s  
28.07.2023 12:53

■ Maximum Principal  
■ Middle Principal  
■ Minimum Principal

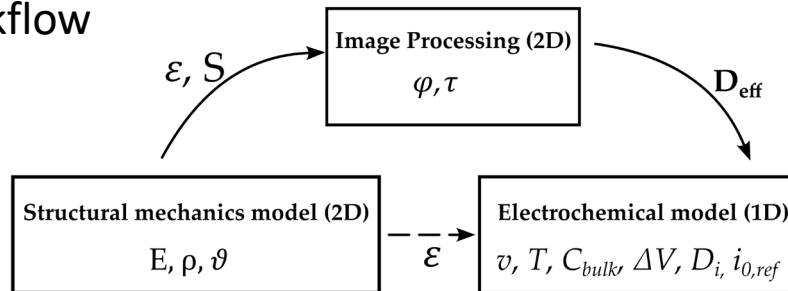


- How will the SSC electrochemical performance change under load conditions?

**need for a mechanical-electrochemical model!**

# Methodology

- Modeling workflow

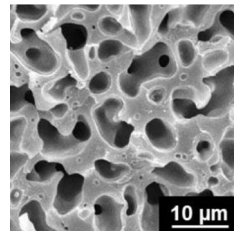


- Computational homogenization



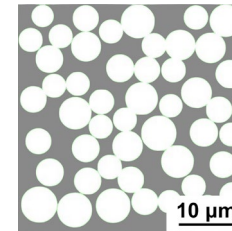
Electrolyte sample

RVE

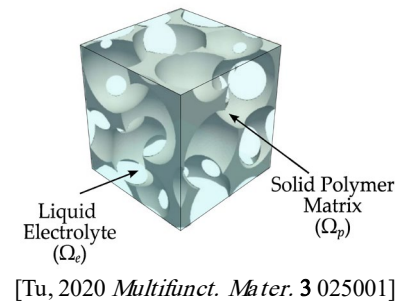


SEM image microstructure

numerical regeneration



inverse bead model



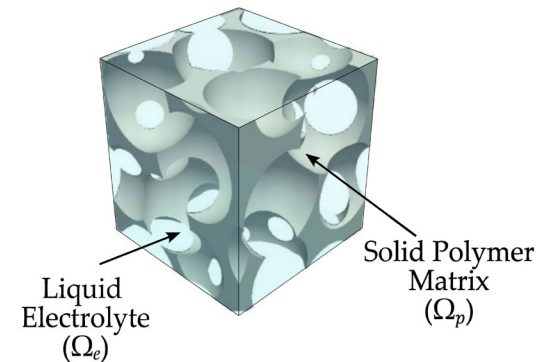
# Governing equations

2D Linear Elastic Model (in  $\Omega_p \times \mathbb{R}^+$ )

$$\nabla \cdot \mathbf{S} + \mathbf{F}_V = 0$$

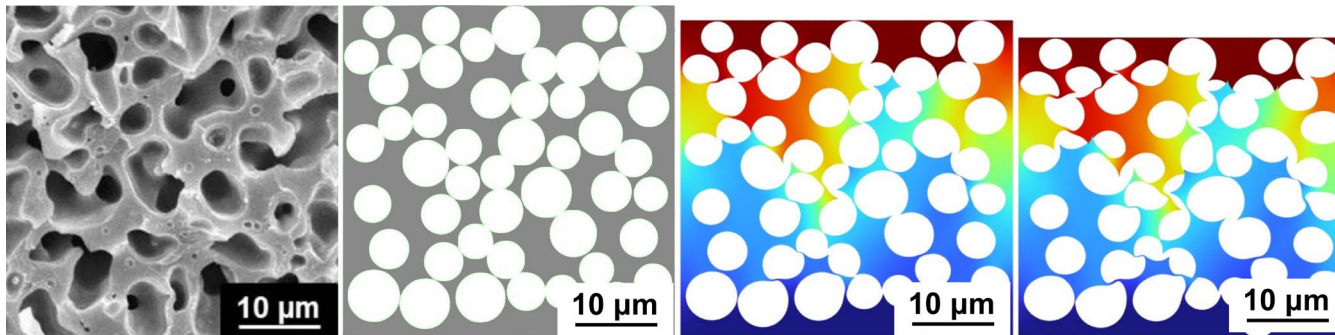
$$\boldsymbol{\varepsilon} = \frac{1}{2} [\nabla \mathbf{u} + (\nabla \mathbf{u})^T]$$

$$\mathbf{S} = \mathbf{C} : \boldsymbol{\varepsilon}$$



[Tu, 2020 *Multifunct. Mater.* 3 025001]

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SEM image of the  
bicontinuous SPE

inverse bead RVE

deformation plots at  $\varepsilon=5\%$ , and  $\varepsilon=10\%$



# Governing equations

2D Linear Elastic Model (in  $\Omega_p \times \mathbb{R}^+$ )

$$\nabla \cdot \mathbf{S} + \mathbf{F}_V = 0$$

$$\boldsymbol{\varepsilon} = \frac{1}{2} [\nabla \mathbf{u} + (\nabla \mathbf{u})^T]$$

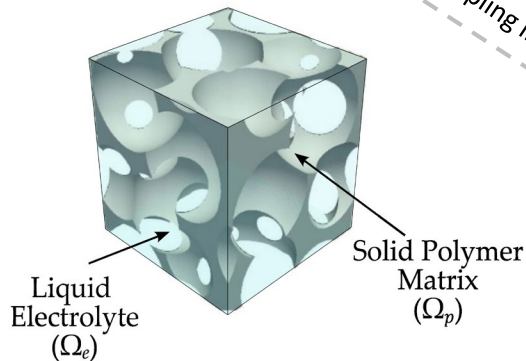
$$\mathbf{S} = \mathbf{C} : \boldsymbol{\varepsilon}$$

one-way coupling?

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direct coupling in COMSOL?



1D Electro-Diffusion CV Model (in  $\Omega_e \times \mathbb{R}^+$ )

$$\phi_l = 0$$

$$\frac{\partial c_i}{\partial t} = D_i \frac{\partial c_i}{\partial x}$$

$$i_{loc} = nFk_0 \left( c_A \exp\left(\frac{(n-\alpha_c)F\eta}{RT}\right) - c_B \exp\left(\frac{-\alpha_c F\eta}{RT}\right) \right)$$

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# Governing equations

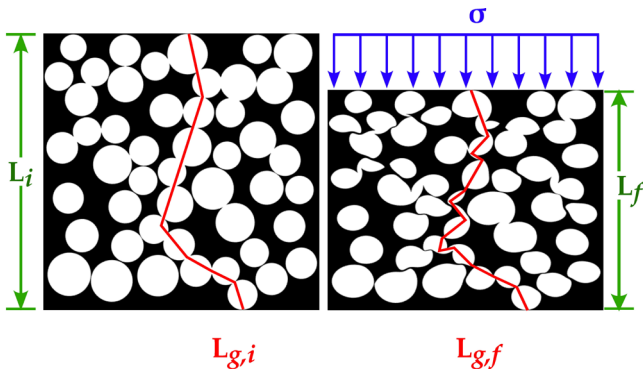
2D Linear Elastic Model (in  $\Omega_p \times \mathbb{R}^+$ )

$$\nabla \cdot \mathbf{S} + \mathbf{F}_V = 0$$

$$\boldsymbol{\varepsilon} = \frac{1}{2} [\nabla \mathbf{u} + (\nabla \mathbf{u})^T]$$

$$\mathbf{S} = \mathbf{C} : \boldsymbol{\varepsilon}$$

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python™ ImageJ  
Image Processing and Analysis in Java

Diffusion (in  $\Omega_e \times \mathbb{R}^+$ )

$$\frac{\partial c_i}{\partial t} = D_i \frac{\partial c_i}{\partial x} \quad \varphi = \frac{A_{pore}}{A_{total}}$$

$$D_{\hat{c}} = \kappa D : \mathbf{M} \mathbf{C}$$

$$\kappa = \frac{\varphi}{\tau} \quad \tau = \frac{L_g}{L}$$

1D Electro-Diffusion CV Model (in  $\Omega_e \times \mathbb{R}^+$ )

$$\phi_l = 0$$

$$\frac{\partial c_i}{\partial t} = D_i \frac{\partial c_i}{\partial x}$$

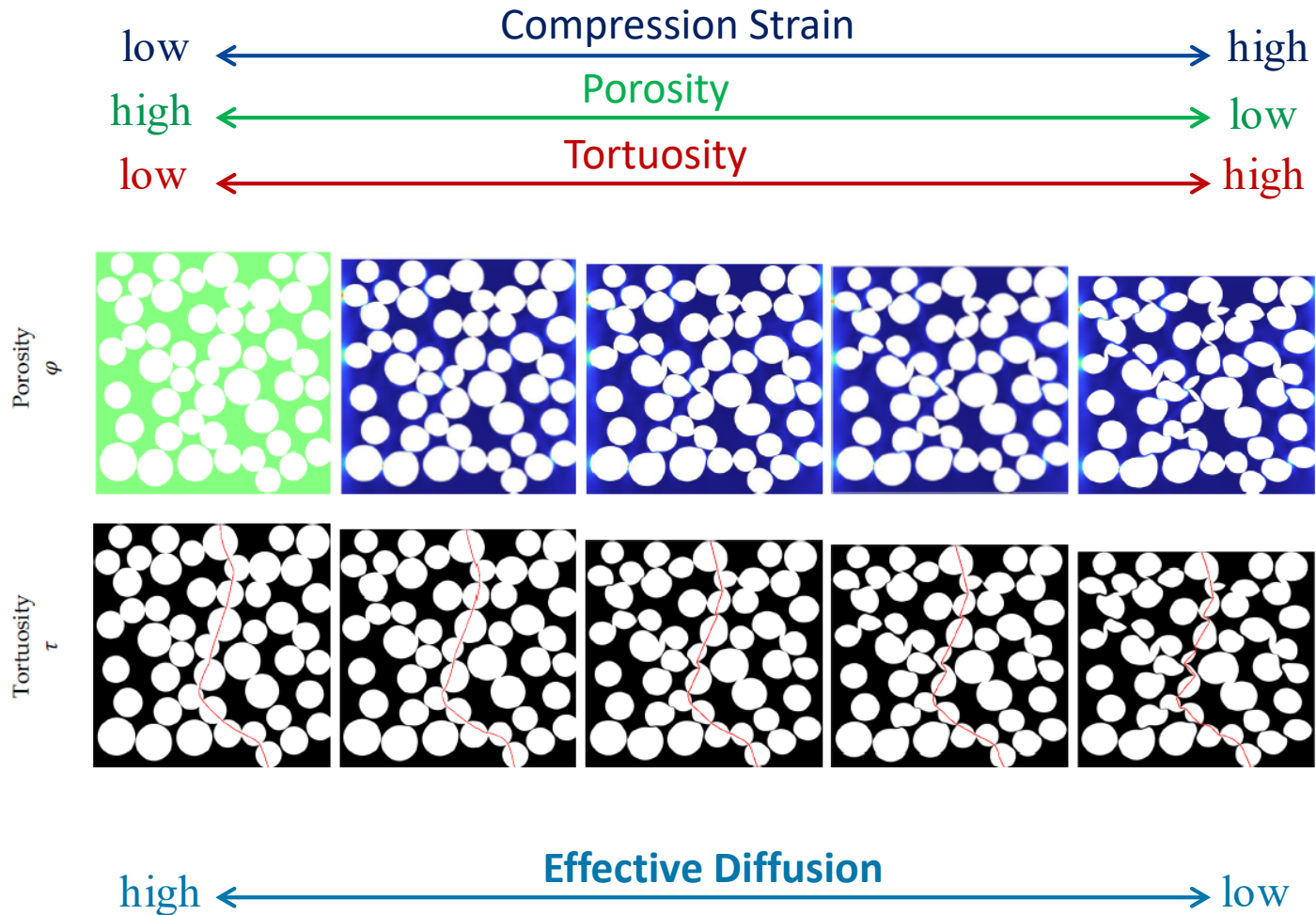
$$i_{loc} = nFk_0 \left( c_A \exp\left(\frac{(n-\alpha_c)F\eta}{RT}\right) - c_B \exp\left(\frac{-\alpha_c F\eta}{RT}\right) \right)$$

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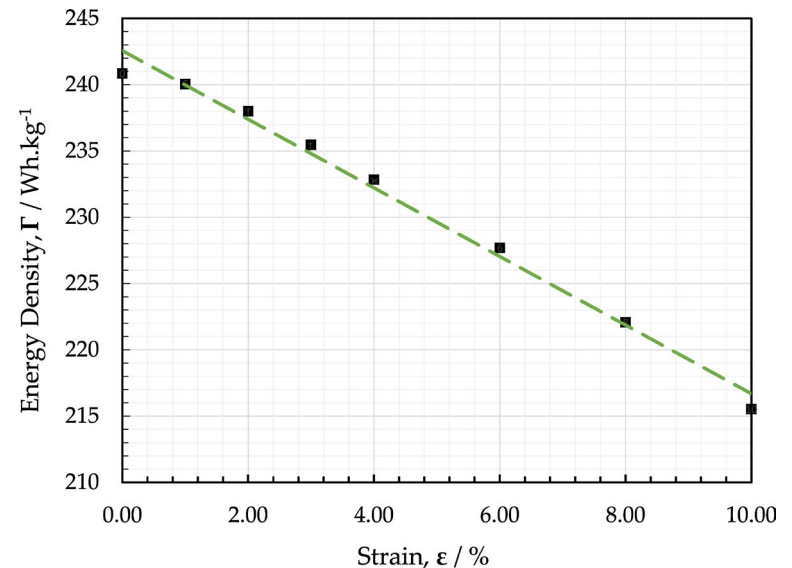
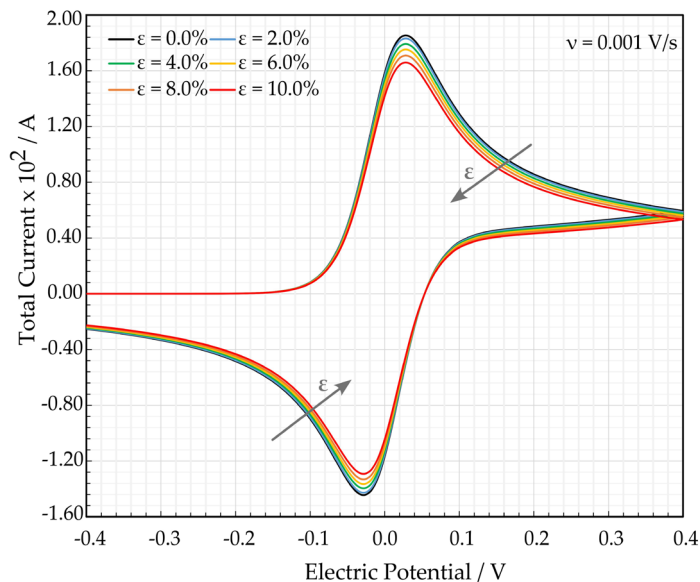
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# Results and Discussion



# Results and Discussion

Compressive strain leads to morphological changes in SE →  
effective diffusion reduction →  
lower specific capacitance (shrinking CV diagrams)



increasing the compression strains to 10% → 12% reduction in SSC energy density!

# Conclusion

- Structural supercapacitors as game changers for future lightweight high-power applications.
- Proposition of a model to investigate the mechanical-electrochemical coupling in a structural supercapacitor with a bicontinuous polymer electrolyte.
- A one-way coupling introduced using FEA and image processing techniques.
- The results showed that increasing the compressive strains up to 10% lowers the energy density of the SSC by around 12%.
- Future efforts will focus on validating the model with experimental data.

# Research Team

*Leipzig University of Applied Sciences (HTWK)*

## Composite Lightweight Engineering Group



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Prof. Dr. Robert Böhm



Group leader  
Dr. Michael Kucher



Research Associate  
Davood Peyrow Hedayati



Undergraduate student  
Gabriel Kahlmeyer

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*Thank you for your attention!*

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